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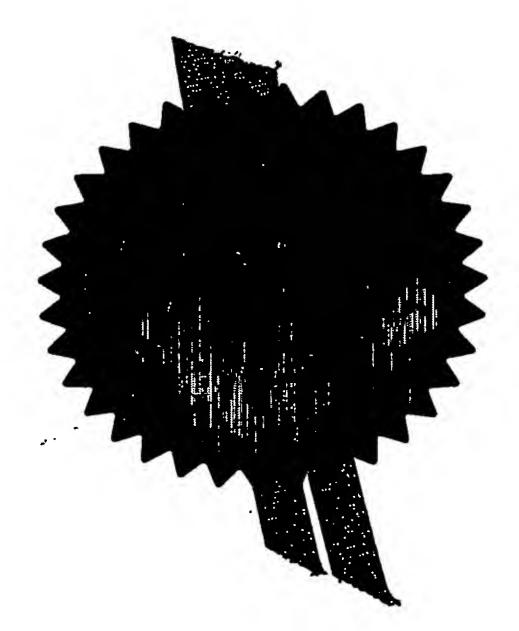
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Claims(s)

Abstract

Drawing(s) $10 + l \vartheta$

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CONTROL SYSTEM FOR CRAFT AND A METHOD OF CONTROLLING CRAFT

The present invention relates to a control system for craft and a method of controlling craft.

Background of the Invention

In conventional aircraft, the pilot sets the wing flap for landing configuration, take-off or go-around. He then uses elevator control to trim and pitch the aircraft according to requirement i.e. flare into landing or pull up into take-off.

One type of conventional missile has a fixed main wing and a movable tail surface. Another type of conventional missile has a smaller forward movable canard as a front surface, and a larger wing behind it.

Summary of the Invention

According to the present invention, there is provided a control system for craft having a main wing control surface and a secondary wing control surface, the system comprising synchronised operation of the main wing control surface and the secondary wing control surface.

The control system of the present invention may include any one or more of the following preferred features:-

- synchronised operation provides identical rotational and/or translational movement of the main and secondary control surfaces;
- synchronised operation provides proportional rotational and/or translational movement of the main and secondary control surfaces;
- synchronised operation provides geared rotational and/or translational movement of the main and secondary control surfaces;

- synchronised operation provides variable rotational and/or translational movement of the main and secondary control surfaces;
- the craft comprises more than one main wing control surface and/or more than one secondary wing control surface;
- substantially all the control surface of the main wing and/or the secondary wing is moveable under the synchronised operation;
- a flap portion of the main wing control surface is moveable under the synchronised operation;
- the craft comprises an aircraft or a marine craft or a missile or a torpedo;
- the craft is unmanned;
- means to off-set the body axis relative to the instantaneous flight path velocity vector;
- means to effect an applied manoeuvre about an instantaneous zero lift line;
- means to maintain constant speed V;
- means to adjust, at predetermined time intervals, the control surfaces setting to effect configuration of the zero lift line manoeuvre.

Preferably, the gearing between the main and secondary wing surfaces (e.g. wing and tail control) deflection is variable. As such it is considered to be a soft control. The ratio of the wing to control deflection is aimed purely at controlling the zero lift line on a continuous basis to improve seekermaintained lock onto the target under manoeuvre of the craft, as well as to achieve ideal terminal trajectory shaping in order to impact the target with a high probability of kill.

Thus, when a complete wing is deflected as a control surface, the local wing+body combined zero lift line is changed. The same argument applies to a fully moving tail in combination with the body. Where the two move as in the current invention, then the overall body experiences a change in zero lift line. Fully moving surfaces are in keeping with missile methods of control.

In cases where the wing and tail is fixed to the body with only a trailing edge flap offering control, the lifting surface to which it is attached experiences a local change in zero lift line similar to that for a fully moving surface as the flap is deflected. If both the wing and tail surface comprise trailing edge flaps, then there is again an overall body change in zero lift line due to the combined effect of deflecting one or both sets of controls in any order. Lifting surfaces, whether acting as a wing or tail surface which operate a trailing edge flap, are more in keeping with UAV's and civil/military aircraft.

The present invention also provides a craft having a control system of the present invention.

According to the present invention, there is also provided a method of controlling a craft having a main wing control surface and a secondary wing control surface, the method comprising synchronising operation of the main wing control surface and the secondary wing control surface.

The method may include any one or more of the following preferred features:-

- identical rotational and/or translational movement of the main and secondary control surfaces;
- proportional rotational and/or translational movement of the main and secondary control surfaces;
- geared rotational and/or translational movement of the main and secondary control surfaces;
- varied rotational and/or translational movement of the main and secondary control surfaces;
- moving more than one main wing control surface and/or more than one secondary wing control surface;
- moving substantially all the control surface of the main wing and/or the secondary wing under the synchronised operation;

- moving a flap portion of the main wing control surface and/or of the secondary wing control surface under the synchronised operation;
- the craft being an aircraft, or a marine craft, or a missile, or a torpedo;
- off-setting the body axis relative to the instantaneous flight path velocity vector;
- effecting an applied manoeuvre about an instantaneous zero lift line;
- maintaining constant speed V;
- adjusting at predetermined time intervals, the control surfaces settings to effect configuration of the zero lift line manoeuvre;
- controlling, selectively as required, to provide:

constant speed;

variable speed;

proportional rotational and/or translational movement of control surfaces;

geared rotational and/or translational movement of control surfaces; variable rotational and/or translational movement of control surfaces.

According to the present invention, there is also provided a computer program product directly loadable into the internal memory of a digital computer, comprising software code portions for performing the method of the present invention when said product is run on a computer.

According the present invention, there is also provided a computer program directly loadable into the internal memory of a digital computer, comprising software code portions for performing the method of the present invention when said program is run on a computer.

According to the present invention, there is also provided a carrier, which may comprise electronic signals, for a computer program embodying the present invention.

According to the present invention, there is also provided electronic distribution of a computer program product, or a computer program, or a carrier of the present invention.

Advantages of the Present Invention.

The present invention as described herein may provide the following advantage of greater control over body angle of attack during flight which enables configuring the airframe for optimal fuel efficiency. In this way, the present invention may extend range or improve ground seeker sweep area for target acquisition and height holding/terrain following functions.

When used in missiles or torpedoes, the present invention may provide one or more of the following advantages:-

Maintaining manoeuvreability right down to impact, with zero grazing incidence at impact. This improves warhead probability of kill and so improved warhead efficiency;

Better shaping of terminal trajectory with higher probability of impacting the target at lower angles to the vertical, thereby improving probability of kill at impact due to improved warhead efficiency;

Improved terminal performance upon impact (for both fixed and moving targets);

Greater control over the missile into the terminal phase trajectory. Thus there is an improved ability to maintain "lock-on" of the seeker equipment onto the target without the loss which usually results from the seeker hitting look angle limits;

Longer time for doing the processing operations to determine if a "locked-onto" target is hostile or friendly;

Actuating a wing under constant or variable flight speed control to reduce the need for significant actuation torque, resulting in reduction of the size and cost of actuation mechanism.

In the present invention, the body incidence (angle between axis of symmetry and flight path vector) can be zero leaving the inter-linked wing and tail surfaces under deflection to achieve the required manoeuvre g by providing the necessary latax force.

Applications of the Present Invention

The present invention is applicable to aircraft, marine craft, missiles, torpedoes and unmanned airborne vehicles (UAV).

General Description of the Present Invention

In order that the present invention may more readily be understood, a description is now given, by way of example only, reference being made to the accompanying drawings, in which:

Figure 1A is a schematic drawing of a missile with a conventional control system;

Figure 2A shows the missile of Figure 1 in an impact manoeuvre;

Figure 3A shows the trajectory of the missile of Figure 1;

Figures 4A, 5A and 6A show schematically other features of a conventional missile;

Figures 1B to 6B show equivalent situations for a missile of the present invention;

Figure 7 shows another trajectory of a missile;

Figure 8 shows the trajectory of a conventional missile;

Figure 9 is a further trajectory of a missile embodying the present invention; and

Figures 10 to 13 show a more detailed trajectory of a missile of the present invention.

The present invention provides a wing and tail inter-linked control system to improve overall performance of a craft, for example an aircraft, especially a missile or torpedo.

To accomplish this, a method of control is implemented by use of an algorithm which, although derived in generic form, is here demonstrated by a specific example. While the example of algorithm given involves a constant speed, of course the present invention includes algorithms involving variable speeds.

The term "inter-linked" control refers to a system whereby the wing and tail control surfaces are operated to move relative to each other to effect a manoeuvre of the airframe, while simultaneously offsetting the body axis relative to the instantaneous flight path velocity vector.

The method of control proposes that, in any actuation of the wing and tail, the craft (or missile) essentially exhibits an applied manoeuvre about an instantaneous zero lift line (ZLL). This feature, and the benefits it affords over conventional flight of craft, for example aircraft or missiles, is a major beneficial consequence of the present invention. There are also consequential benefits for weapon control systems which utilise missiles of the present invention.

Figure 1A shows schematically a conventional missile 1 with a fixed wing 2 and a fully moving tail 3. Missile 1 manoeuvres by rotating the body axis relative to the flight path using aft tail control surface 3.

Figure 2A shows schematically missile 1 as it manoeuvres primarily due to body angle of attack showing a grazing incidence at impact.

Figures 1B, 2B, and 3B show corresponding situations but for a missile 11 embodying a control system of the present invention having a moving wing 12 with a link to control a moving tail 13. Missile 11 manoeuvres relative to the zero lift line (ZLL) by rotation of both wing and tail surfaces. ZLL is selectable based on airframe aerodynamics to achieve improved missile look angle on target while maintaining appropriate manoeuvre. Missile 11 is subject to reduced manoeuvre stall limit over the conventional missile 1 above.

If the flight path velocity vector is co-incident with the Zero Lift Line, then there is no net aerodynamic lift generated on the airframe.

Thus Figure 2B shows a manoeuvre achieved by combined deflection of wing 12 and tail 13 at zero angle of attack which provides no grazing incidence at impact.

Figure 3B indicates the benefits of the present invention over the situation shown in Figure 3A of a conventional missile 1, whereby missile 11 provides a shorter acquisition range, a better shaped trajectory, potential to improve target top attack (by an improved potential to kill the target), better maintaining target lock-on throughout flight, and better acquisition of targets whether fixed or moving.

In Figure 3B, the body altitude/ZLL of missile 11 is selected to maintain target lock-on throughout flight while maintaining trajectory manoeuvre.

Figure 4B shows that missile 11 achieves the same low g manoeuvre with an improved look angle onto target 4, although the absolute manoeuvre g is stall-limited at a lower level.

Figure 5A shows the trajectory of missile 1 in an anti-ship implementation as it approaches target 4, involving a significant variation in Radar Cross-Section (RCS), this being typical of conventional missile 1.

In Figure 5B, there is shown an RCS remaining reasonably steady even during manoeuvre to produce a confusing trajectory RCS return.

Figure 6B indicates that the present invention allows missile 11 to manoeuvre with air intake in line with air flow, providing enhanced efficiency of fuel consumption, allowing increased range or less fuel for a given distance optionally allowing increased pay load.

Figure 7 is a detailed schematic diagram of the terminal engagement trajectory of missile 11 including an initial pull-up, followed by a bunt manoeuvre down to the target. Prior to target acquisition (i.e. the locking of the missile on to the target), it is assumed that the attacking missile uses its seeker equipment to establish its own ground speed and cruise height and then processes the returns from the target to identify target speed and direction.

The initial pull-up manoeuvre starts at point "A" with the attacking missile assumed beginning the pull-up phase at a steady cruise height above ground level with the seeker equipment locked onto the target. For this example, it is assumed that both the attacking missile and the target are travelling in the plane of manoeuvre i.e. the pitch plane.

Figure 8 illustrates what occurs in conventional missiles with fixed-wing and moving tail control surfaces whereby the pull-up phase risks losing lock with the target as the demand manoeuvre forces the missile seeker towards look-angle limits as the airframe puts on angle of attack.

This is particularly a risk with the target moving towards the attacking missile as the closing speed increases. To remedy this, a shallower trajectory may be initiated which, while offering reduced exposure to counterattack at altitude, reduces the impact angle with the target due to limited manoeuvre response time in completing the bunt.

This in turn limits warhead effectiveness, as the attitude at target intercept tends to be shallow. It also follows that, if the missile is still manoeuvring at target impact, then the airframe must put on incidence. This in turn implies that the missile grazing incidence will potentially be high, again limiting warhead effectiveness. Breaking away from the bunt manoeuvre during descent to the target allows the airframe to reduce grazing incidence at target impact, but at the expense of acquisition range prior to target lock-on.

This in turn either reduces the time available to process data to confirm the target as a threat prior to "lock-on", or again forces subsequent bunt manoeuvre (post "lock-on") to be shallow, due to reduced time of flight to impact the target.

To counter limitations posed by the conventional fixed-wing moving-tail missile, the present invention provides a moving wing and tail combination by an inter-linked (geared) electronic actuation control mechanism (see Figure 9).

Latax manoeuvre may be achieved by deflecting the wing and tail relative to the missile body centreline in order that the line of zero lift acts off of the missile axis. Manoeuvre is then initiated relative to this line. In the "pull-up" phase, this enables the body to fly with negative body axis incidence but with the combined wing and tail deflection offering positive relative angle of attack to the flight vector to provide the required manoeuvre g.

In this configuration, the manoeuvre is maintained but with a reduced "look-angle" to the target. Clearly this offers a reduced risk of the sightline hitting stops during pull-up which would otherwise result in loss of target "lock-on".

This method of control affords additional flexibility to ensure greater freedom to shape the terminal bunt trajectory. At the apogee of the bunt manoeuvre, it may be advantageous to resort to similar control methods as those of the fixed wing design, since increased negative angle of attack to achieve positive manoeuvre g ensures that the look angle is reduced onto the target (note the convention here for +ve manoeuvre g in Figures 8 and 9 in particular).

However, during the descent phase, it is of major benefit to manoeuvre without pulling incidence, particularly in the last few seconds of flight.

Achieving this down to the target means that impact can be achieved with zero grazing incidence, thus ensuring optimal warhead efficiency. It further follows that the target impact angle will naturally be lower to the vertical again enhancing warhead efficiency. It should be noted in Figure 9 that in addition to the zero lift line and associated angle, there is an additional incidence. This represents the more general case of incidence error in achieving an absolute zero light angle with flight vector along the flight path. Ideally, this "alpha" error is driven to zero in achieving the present invention and its inclusion in Figure 9 is to present the more general case rather that the absolute ideal.

The detailed implementation provides the aforementioned benefits of the present invention including trajectory shaping and maintained look angle on the target, with the consequential advantages of optimising target impact warhead effectiveness.

The implementation encapsulates the generic trajectory shape in Figure 7 formulated via a series of defining geometric parameters. This generic or idealistic trajectory shape comprises two arcs of a circle, with interface at the point where the trajectory leaves the "pull-up" phase and enters the terminal bunt. Throughout flight the missile is controlled to maintain constant speed V so that, despite continuity of climb angle at the interface of the two phases of flight, there is a step change in manoeuvre g from —ve in the "pull-up" to +ve in the bunt.

Two types of target are considered: fixed and moving. For a fixed target at "T0", the attacking missile is assumed able to acquire the target beyond point "A". With the target confirmed and "lock-on" achieved before point "A", the missile travelling at constant speed "V" enters the terminal engagement trajectory by performing a pull-up manoeuvre at constant climb rate (constant radius of turn). At some point into climb "C", the engagement algorithm signals that the airframe requires "limit manoeuvre g" to intercept the target. If the airframe subsequently executes a circular arc to intercept the target, the flight vector is at zero degrees to the vertical if the instantaneous centre of rotation in the bunt (point "O") rests on the ground line coincident with the target. If the target is moving towards the attacking missile then it follows that, if "limit manoeuvre g" is not to be exceeded in intercepting at a biased and fixed aim point ahead of the target, the missile must leave the "pull-up" phase earlier than for the fixed target i.e. at point "M0".

In this case, however, because the missile must not exceed "limit manoeuvre g", the instantaneous centre of rotation must be at a point close to "OT3", off the ground line.

Clearly the choice of points "M0" and the instantaneous point of rotation varies with speed of the target for the limit manoeuvre g, and must ensure that the time of flight from "A" to intercept the target coincides with the time the target takes to travel from "T0" to intercept. The target is locked onto at A. At this point, the target is T0. By the time the missile has flown the trajectory path i.e. pull up and pull down (bunt) the target will have travelled from T0 to meet up with the missile i.e. the two achieve intercept. In this case, it follows that the flight path vector at impact is greater than zero degrees angle to vertical. If it is assumed that the missile breaks away from the pull-up phase at point "M0" to intercept a fixed target at "T0" (trajectory T0') "manoeuvre g" will be below the "limit manoeuvre g" for the airframe.

From Figure 7 it also follows that if the missile breaks away from the pull-up phase at point "M0" with a turning circle equal to that required to intercept a fixed target at "T0", and the radius of turn is progressively reduced by migrating the instantaneous centre of rotation along the line "OT' – OT3" (such that the radius from the attacking missile to the instantaneous centre of rotation is equal to the radius from the instantaneous centre of rotation to the target), the missile will progress an arc through radii R1, R2, R3 etc at positions M1, M2, and M3 down to intercept with increasing manoeuvre g.

Note here that the loci of the instantaneous centres of rotation lie on the extended radius through the missile location at the time of breakaway from the pull-up manoeuvre. Throughout the subsequent trajectory, the "instantaneous manoeuvre g" is assumed to act normal to the flight path along the instantaneous radius with the constant velocity normal to this radius.

The instantaneous sightline is then the angle between the normal to the radius and the chord of the arc of the instantaneous manoeuvre circle between the missile and target for zero angle of attack.

The steady State Trim Condition

The benefits of the present invention may be summarised via analysis of the simple steady state trim condition for the present invention and conventional systems.

The Conventional Missile with a Fixed Wing+Moving Tail System

Taking moments about the instantaneous C of G,

$$Cm_{cg} = Cm_{cg_a}.\alpha + Cm_{cg_{\delta_i}}.\delta_i$$
 1

For the Normal Force Coefficient in body fixed axes,

$$C_N = C_{N_a} \alpha + C_{N_{\delta_i}} \delta_i \qquad 2$$

For a missile in instantaneous trim [Cmcg = 0] with mass m, speed V, the trim incidence α and tail control deflection δt are derived as follows

$$\alpha = \left[\frac{m.n_g.g}{\frac{1}{2}\rho V^2 S}\right] \left[\frac{Cm_{cg_a}}{(C_{N_a}.Cm_{cg_a} - C_{N_a}.Cm_{cg_a})}\right]$$
 3

and,

$$\delta_{t} = -\left[\frac{m.n_{g}.g}{\frac{1}{2}\rho V^{2}S}\right]\left[\frac{Cm_{cg_{\alpha}}}{(C_{N_{\alpha}}.Cm_{cg_{\alpha}} - C_{N_{\alpha}}.Cm_{cg_{\alpha}})}\right] \qquad 4$$

Clearly from the first of these two equations demanding a manoeuvre requires angle of attack and this determines the tail deflection required to achieve it at the associated instantaneous trim state.

The Method of Control of the present invention e.g. with an Interlinked Wing+Tail

Taking moments about the instantaneous C of G,

$$Cm_{cg} = Cm_{cg_{\alpha}}.\alpha + Cm_{cg_{\delta_{\psi}}}.\delta_{\psi} + Cm_{cg_{\delta_{t}}}.\delta_{t}$$
 5

For the Normal Force Coefficient in body fixed axes,

$$C_N = C_{N_\alpha}.\alpha + C_{N_{\delta_w}}.\delta_w + C_{N_{\delta_l}}.\delta_l$$
 6

For conditions along the zero lift line (ZLL) $Cm_{cg}=0$ and $C_N=0$, $\alpha=\alpha_0$, $\delta_W=\delta_{W0}$ and $\delta_t=\delta_{t0}$, thus

$$\begin{bmatrix} Cm_{cg_{\delta_{w}}} & Cm_{cg_{\delta_{t}}} \\ C_{N_{\delta_{w}}} & C_{N_{\delta_{t}}} \end{bmatrix} \begin{bmatrix} \delta_{w_{0}} \\ \delta_{t_{0}} \end{bmatrix} = -\begin{bmatrix} Cm_{cg_{\alpha}} \\ C_{N_{\alpha}} \end{bmatrix} \alpha_{0}$$
 7

or after solution,

$$\begin{bmatrix} \delta_{w_0} \\ \delta_{t_0} \end{bmatrix} = \frac{\begin{bmatrix} Cm_{cg_{\delta_l}}.C_{N_a} - C_{N_{\delta_l}}.Cm_{cg_a} \\ C_{N_{\delta_w}}.Cm_{cg_a} - Cm_{cg_{\delta_w}}.C_{N_a} \end{bmatrix}}{(Cm_{cg_{\delta_w}}.C_{N_{\delta_l}} - C_{N_{\delta_w}}.Cm_{cg_{\delta_l}})} \alpha_0 = \begin{bmatrix} F_1 \\ F_2 \end{bmatrix} \alpha_0$$
 8

Note here that KGw_0 (the ratio of tail to wing control deflection at zero lift) is defined as,

$$KG_{w_0} = \frac{F_2}{F_1} = \frac{\delta_{t_0}}{\delta_{w_0}}$$

If one changes to wind axes,

$$Cm_{cg} = Cm_{cg_{\alpha}} \cdot (\alpha - \alpha_0) + Cm_{cg_{\delta_{w}}} \cdot (\delta_{w} - \delta_{w_0}) + Cm_{cg_{\delta_{t}}} \cdot (\delta_{t} - \delta_{t_0})$$
 10

and,

$$C_{N} = C_{N_{\alpha}} \cdot (\alpha - \alpha_{0}) + C_{N_{\delta_{w}}} \cdot (\delta_{w} - \delta_{w_{0}}) + C_{N_{\delta_{t}}} \cdot (\delta_{t} - \delta_{t_{0}})$$
 11

It is assumed that the zero lift angle from the missile is sufficiently small that the normal force coefficient acting along the normal to the ZLL differs little from that acting normal to the missile body centreline.

Consider now all three angles to change relative to the conditions for zero lift i.e., for body angle of attack, $\alpha \to \alpha_0 + \alpha'$, $\delta w \to \delta w_0 + \delta w'$ and $\delta t \to \delta t_0 + \delta t'$ after substitution,

$$Cm_{cg} = Cm_{cg_{\alpha}}.\alpha' + Cm_{cg_{\delta_{w}}}.\delta'_{i\nu} + Cm_{cg_{\delta_{t}}}.\delta'_{t}$$
 12

and

$$C_N = C_{N_{\alpha}}.\alpha^{\dagger} + C_{N_{\delta_{w}}}.\delta^{\dagger}_{w} + C_{N_{\delta_{t}}}.\delta^{\dagger}_{t}$$
 13

Again in the trim state, $Cm_{cg} = 0$ but under a demand manoeuvre, $C_N \neq 0$ and we find that,

$$\delta_{t}' = -\frac{\left(Cm_{cg_{a}}.\alpha' + Cm_{cg_{\delta_{w}}}.\delta_{w}'\right)}{Cm_{cg_{\delta_{t}}}}$$
14

and,

$$C_{N} = \frac{mn_{g}.g}{\left(\frac{1}{2}.\rho V^{2}S\right)} = \frac{\left[C_{N_{a}}.Cm_{cg_{\delta_{i}}} - C_{N_{\delta_{i}}}.Cm_{cg_{a}}\right]\alpha^{i} + \left[C_{N_{\delta_{w}}}.Cm_{cg_{\delta_{i}}} - C_{N_{\delta_{i}}}.Cm_{cg_{\delta_{s}}}\right]\delta^{i}_{w}}{Cm_{cg_{\delta_{i}}}}$$
 15

 $\alpha' = 0$ to yield,

$$\delta'_{t} = -\left(\frac{Cm_{cg_{\delta_{w}}}}{Cm_{cg_{\delta_{t}}}}\right)\delta'_{w} = KG_{w}.\delta'_{w}, \quad KG_{w} = -\left(\frac{Cm_{cg_{\delta_{w}}}}{Cm_{cg_{\delta_{t}}}}\right) > 0 \quad 16$$

In setting $\alpha' = 0$, it is assumed that the missile is controlled to achieve an incidence α_0 . This is a by-product of the inter-linked control system employed. In reality the existence of α' surfaces due to errors in achieving α_0 under natural control via the guidance and control loop.

With the assumption of the ideal case $\alpha' = 0$ it then follows that,

$$\delta_{w} = \delta_{w_0} + \delta'_{w} = F_1 \cdot \alpha_0 + \frac{\left(\frac{m \cdot n_g \cdot g}{1 \cdot \rho \cdot V^2 S}\right) \cdot Cm_{cg_a}}{\left(C_{N_{sr}} \cdot Cm_{cg_a} - C_{N_a} \cdot Cm_{cg_{sr}}\right)}$$
17

$$\delta_{t} = \delta_{t_0} + \delta_{t}^{t} = F_{2} \alpha_{0} + KG_{w} \cdot \frac{\left[\frac{m n_{g}.g}{\frac{1}{2}.\rho.V^{2}S}\right].Cm_{cg_{a}}}{\left(C_{N_{de}}.Cm_{cg_{a}} - C_{N_{a}}.Cm_{cg_{de}}\right)}$$
18

Note the important point here that manoeuvre can be achieved by moving the wing and tail either with or without incidence α_0 .

Simplifying these expressions,

$$\delta_{w} = F_{1}\alpha_{0} + K n_{g} \qquad 19$$

and,

$$\delta_t = F_2 \alpha_0 + K G_w K n_g \qquad 20$$

where,

$$K = \frac{\left(\frac{m.g}{\frac{1}{2} \cdot \rho \cdot V^2 S}\right) \cdot Cm_{cg_a}}{\left(C_{N_{\delta s}} \cdot Cm_{cg_a} - C_{N_{\delta}} \cdot Cm_{cg_{\delta s}}\right)}$$
 21

Rearranging,

$$KG_{w_0} = \frac{F_2 \alpha_0}{F_1 \alpha_0} = \frac{F_2}{F_1} = \frac{\delta_t - KG_w.K.n_g}{\delta_w - K.n_g}$$
 22

and hence,

$$n_{g} = \frac{(KG_{w_{0}}.\delta_{w} - \delta_{t})}{(KG_{w_{0}} - KG_{w}).K} = \delta_{w} \frac{(KG_{w_{0}} - KG_{w}')}{(KG_{w_{0}} - KG_{w}).K}$$
23

where,

$$KG_{w}' = \frac{\delta_{t}}{\delta_{w}} = \left(\frac{KG_{w_{0}} + KG_{w}.\tau}{1+\tau}\right) \quad , \quad \tau = \frac{\delta_{w}'}{\delta_{w_{0}}} = \left(\frac{\delta_{w} - \delta_{w_{0}}}{\delta_{w_{0}}}\right)$$
 24

Thus if $\delta'_w = 0$, $\tau = 0$ and $KG_w'=KG_{w0}$ which implies a default to the zero lift line (ZLL) where the manoeuvre g is zero. This checks since in this case, substituting for $KG_w'=KG_{w0}$ sets $n_g=0$.

After substitution and rearrangement,

$$n_g = \frac{\delta'_w}{K} \qquad 25$$

which again confirms the same result that $n_g = 0$ when $\delta'_w = 0$.

From a control point of view, it is more useful to use full wing control deflection and that associated with zero lift conditions, therefore the more appropriate form of expression for n_g is,

$$n_{g} = \frac{(\delta_{w} - \delta_{w_0})}{K}$$
 26

Note that the choice of ZLL angle is arbitrary being restricted only by the stall condition primarily on the wing but also the tail. This lends itself to the possibility of demanding an effective ZLL angle which complies with sightline look angle limits while satisfying manoeuvre g requirements and lifting surface stall angle limitations.

<u>Definition of Terminal Engagement Algorithm to negotiate both Fixed and Moving Targets.</u>

Mathematical Analysis - Defining The Generic Engagement Algorithm

The terminal engagement trajectory is assumed comprised of two phases, a pull-up phase and a bunt phase.

In order to progress mathematical definition of the algorithm the schematic form of the terminal engagement trajectory in Figure 10 is adopted and introduce necessary axis conventions and terminology that will be adopted throughout the ensuing analysis

Trajectory Kinematics-PULL-UP Phase

Transformation matrices defined in APPENDIX 1 are used throughout the ensuing analysis and are based on the conventions defined in Figure 10.

Applying kinematic modelling of the missile using the axes convention of Figure 10, the following matrix relationships between velocities and accelerations defined in rotating axes with instantaneous centre of rotation O_c at radius r_{cp} and those in instantaneous trajectory axes are as follows.

$$\underline{V}_{cp} = \begin{bmatrix} \dot{r}_{cp} & r_{cp} \cdot \dot{\theta}_{cp} \end{bmatrix} \begin{bmatrix} Sin(\theta_{cp}) & -Cos(\theta_{cp}) \\ Cos(\theta_{cp}) & Sin(\theta_{c}) \end{bmatrix} \begin{bmatrix} Cos(\theta_{c}) & Sin(\theta_{c}) \\ Sin(\theta_{c}) & -Cos(\theta_{c}) \end{bmatrix} \begin{bmatrix} \dot{\underline{\iota}}_{traj} \\ \underline{\underline{k}}_{traj} \end{bmatrix}$$

$$\underline{\dot{V}}_{cp} = \begin{bmatrix} \left(\ddot{\underline{\iota}}_{cp} - r_{cp} \cdot \dot{\theta}_{cp}^{2} \right) & \frac{1}{r_{cp}} \frac{\partial}{\partial t} \begin{bmatrix} r_{cp}^{2} \cdot \dot{\theta}_{cp} \end{bmatrix} \end{bmatrix} \begin{bmatrix} Sin(\theta_{c}) & -Cos(\theta_{c}) \\ Cos(\theta_{c}) & Sin(\theta_{c}) \end{bmatrix} \begin{bmatrix} Cos(\theta_{c}) & Sin(\theta_{c}) \\ Sin(\theta_{c}) & -Cos(\theta_{c}) \end{bmatrix} \begin{bmatrix} \dot{\underline{\iota}}_{traj} \\ \dot{\underline{k}}_{traj} \end{bmatrix}$$
28

Hence,
$$\begin{bmatrix} \frac{V}{cp} \\ \frac{v}{cp} \end{bmatrix} = \begin{bmatrix} r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Cos(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Cos(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Cos(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Cos(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) + r_{cp} \theta_{cp} \cdot Sin(\theta_{cp} - \theta_{c}) \\ r_{cp} \cdot$$

Since the trajectory velocities are identical it follows that,

$$\begin{bmatrix} \underline{\underline{V}}_{\mathbf{QP}} \\ \underline{\underline{V}}_{\mathbf{QP}} \end{bmatrix} = \begin{bmatrix} \underline{\underline{V}} \\ \underline{\underline{V}} \end{bmatrix}$$
30

Trajectory Kinematics-bunt Phase

Referring to Figure 10, the following position vector relationships are derived,

$$\underline{r}_{o_{T}} + \underline{r}' = \underline{r}_{1} \qquad 31$$

$$-\underline{r}' + \underline{r}_{T} = \underline{r}_{SL} \qquad 32$$

$$\underline{r}_{o_{T}} + \underline{r}_{T} = \underline{r}_{1} + \underline{r}_{sl} = X_{T} (t^{*} + t) \underline{i} \qquad 33$$

$$\left(r_{cp_{0}} + h_{-} cruise\right) \underline{k}^{-} + r_{cp} \underline{i}_{cp} + r' \underline{k}_{traj} = \underline{r}_{o_{T}} + \underline{r}_$$

Where,

$$\underline{r}_{o_{T}}^{i} = r_{o_{T}}^{i} \underline{i}_{o_{T}}^{i}$$
, $\underline{r}_{1}^{i} = r_{1}^{i}\underline{i}_{1}^{i}$, $\underline{r}_{1}^{i} = r_{1}^{i}\underline{i}_{1}^{i}$, $\underline{r}_{T}^{i} = r_{T}^{i}\underline{i}_{T}^{i}$, $\underline{r}_{sl} = r_{sl}^{i}\underline{i}_{sl}$ 35

If t* is the time into flight at initiation of the pull-up manoeuvre and t is the time thereafter into the terminal phase trajectory then X_T(t*+t), the distance to target impact into the terminal trajectory from commencement of pull-up is given by,

$$X_{T}(t^{*}+t) = X_{T_{0}}(t^{*}) + \int_{t^{*}}^{t^{*}+t} V_{T} dt - \int_{t^{*}}^{t^{*}+t} \frac{\partial}{\partial t} X_{E}(t) dt$$
 36

Where $V_T < 0$ if the target is moving towards the attacking missile, $V_T > 0$ if moving away and V_T=0 if stationary. X_E(t) is the ground range covered by the attacking missile after t secs into flight post entry into the terminal engagement manoeuvre.

If r_{sl}, is the sightline range at target lock-on entering the terminal engagement trajectory then it also follows that,

$$X_{T_0}(t^*) = \sqrt{r_{sl} - h_cruise^2}$$

where,

$$r_{Sl}^{*} = r_{Sl}(t^{*})$$
 38

For the instantaneous centre of rotation at OT', differentiating yields,

or in matrix form,

$$\underline{V}_{o_{T}} = \begin{bmatrix} \dot{r}_{o_{T}}, & r_{o_{T}}, \dot{\theta}_{o_{T}} \end{bmatrix} \begin{bmatrix} \dot{t}_{o_{T}}, & \dot{t}_{o_{T}} \end{bmatrix} = \begin{bmatrix} \dot{r}_{o_{T}}, & r_{o_{T}}, \dot{\theta}_{o_{T}} \end{bmatrix} \begin{bmatrix} \cos(\theta_{o_{T}}, & -\sin(\theta_{o_{T}}, & -\sin(\theta_{o_{T}}, & -\cos(\theta_{o_{T}}, &$$

Differentiating equation 40 then yields the instantaneous centre of rotation acceleration vector to be,

$$\underline{\dot{V}}_{o_{T}^{1}} = \left\{ \left(\ddot{r}_{o_{T}^{1}} - r_{o_{T}^{1}} \dot{\theta}_{o_{T}^{1}}^{2} \right) \cdot Cos(\theta_{o_{T}^{1}}) - \left(r_{o_{T}^{1}} \ddot{\theta}_{o_{T}^{1}} + 2\dot{r}_{o_{T}^{1}} \dot{\theta}_{o_{T}^{1}} \right) \cdot Sin(\theta_{o_{T}^{1}}) \right\}_{\underline{i}} \\
- \left\{ \left(\ddot{r}_{o_{T}^{1}} - r_{o_{T}^{1}} \dot{\theta}_{o_{T}^{1}}^{2} \right) \cdot Sin(\theta_{o_{T}^{1}}) + \left(r_{o_{T}^{1}} \ddot{\theta}_{o_{T}^{1}} + 2\dot{r}_{o_{T}^{1}} \dot{\theta}_{o_{T}^{1}} \right) \cdot Cos(\theta_{o_{T}^{1}}) \right\}_{\underline{k}}^{\underline{k}} \right]$$

$$41$$

For the target the velocity vector $\underline{V}_{\underline{T}}$ is given by,

$$\underline{\underline{V}}_{T} = \dot{\underline{r}}_{T} + \underline{\underline{V}}_{o_{T}} = \dot{\underline{r}}_{T} \cdot \dot{\underline{i}}_{T} + r_{T} \cdot \frac{\partial \underline{i}_{T}}{\partial t} + \underline{\underline{V}}_{o_{T}} = \dot{r}_{T} \cdot \dot{\underline{i}}_{T} + r_{T} \cdot \frac{\partial \underline{i}_{T}}{\partial \theta_{L}} \cdot \frac{\partial \theta_{L}}{\partial t} + \underline{\underline{V}}_{o_{T}} = \dot{r}_{T} \cdot \dot{\underline{i}}_{T} - r_{T} \cdot \dot{\underline{\theta}}_{L} \cdot \underline{\underline{k}}_{T} + \underline{\underline{V}}_{o_{T}}$$

$$42$$

From equation 42,

$$\begin{split} & \underbrace{Y}_{T} = \begin{bmatrix} i_{T} & -r_{T} \cdot \dot{\theta}_{L^{1}} \end{bmatrix} \begin{bmatrix} i_{T} \\ k_{T} \end{bmatrix} + \underbrace{Y}_{OT^{1}} = \begin{bmatrix} i_{T} & -r_{T} \cdot \dot{\theta}_{L^{1}} \end{bmatrix} \begin{bmatrix} Cos(\theta^{1}_{L}) & Sin(\theta^{1}_{L}) \\ Sin(\theta^{1}_{L}) & -Cos(\theta^{1}_{L}) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} + \underbrace{Y}_{OT^{1}} \\ & = \begin{bmatrix} i_{T} & Cos(\theta^{1}_{L}) - r_{L^{1}} \cdot \dot{\theta}_{L^{1}} \cdot Sin(\theta^{1}_{L^{1}}) + r_{T^{1}} \cdot \dot{\theta}_{L^{1}} \cdot Cos(\theta^{1}_{L^{1}}) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} + \begin{bmatrix} i_{T} & Cos(\theta^{1}_{T^{1}}) - r_{OT^{1}} \cdot \dot{\theta}_{OT^{1}} \cdot Sin(\theta^{1}_{OT^{1}}) + r_{OT^{1}} \cdot \dot{\theta}_{OT^{1}} \cdot Cos(\theta^{1}_{OT^{1}}) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} \\ & = \begin{bmatrix} i_{T} & Cos(\theta^{1}_{L^{1}}) - r_{D^{1}} \cdot \dot{\theta}_{L^{1}} \cdot Sin(\theta^{1}_{D^{1}}) + r_{D^{1}} \cdot Cos(\theta^{1}_{D^{1}}) - r_{D^{1}} \cdot \dot{\theta}_{D^{1}} \cdot Sin(\theta^{1}_{D^{1}}) + r_{D^{1}} \cdot Cos(\theta^{1}_{D^{1}}) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} \end{bmatrix} \\ & = \begin{bmatrix} i_{T} & Cos(\theta^{1}_{L^{1}}) - r_{D^{1}} \cdot \dot{\theta}_{L^{1}} \cdot Sin(\theta^{1}_{D^{1}}) + r_{D^{1}} \cdot Cos(\theta^{1}_{D^{1}}) - r_{D^{1}} \cdot \dot{\theta}_{D^{1}} \cdot Sin(\theta^{1}_{D^{1}}) - r_{D^{1}} \cdot \dot{\theta}_{D^{1}} \cdot Cos(\theta^{1}_{D^{1}}) - r_{D^{1}} \cdot \dot{\theta}_{D^{1}} \cdot Cos(\theta^{1}_{$$

Since the target is assumed to travel along the earth fixed x axis, it follows from applying the boundary condition at the ground that

$$\left\{\dot{r}_{T}.Cos(\theta_{L}') - r_{T}.\dot{\theta}_{L}'.Sin(\theta_{L}') + \dot{r}_{O_{T}'}.Cos(\theta_{O_{T}'}) - r_{O_{T}'}.\dot{\theta}_{O_{T}'}.Sin(\theta_{O_{T}'})\right\} = V_{T}$$

$$44$$

and,

$$\dot{r}_T \operatorname{Sin}(\theta_L') + r_T \dot{\theta}_{L'} \operatorname{Cos}(\theta_L') - \dot{r}_{o_T} \operatorname{Sin}(\theta_{o_T'}) - r_{o_T} \dot{\theta}_{o_T'} \cdot \operatorname{Cos}(\theta_{o_T'}) = 0$$

$$45$$

since no velocity normal to the surface exists.

Differentiating this expression and noting that $\underline{i} \underline{k}$ is invariant under differentiation (fixed earth axis unit vectors) it follows that the acceleration of the target in earth axes is given

by,

$$\frac{p}{T} = \left[\left(\left(\tilde{r}_{T} - r_{T} \dot{\theta}_{L}^{-1} \right)^{2} \right) Cos(\theta)_{L}^{-1} \right) - \left(r_{T} \ddot{\theta}_{L}^{-1} + 2\dot{r}_{T} \dot{\theta}_{L}^{-1} \right) Sin(\theta)_{L}^{-1} \right) + \left(\tilde{r}_{O_{T}} - r_{O_{T}} \dot{\theta}_{O_{T}}^{-1} \right) Cos(\theta)_{O_{T}}^{-1} \right) - \left(r_{O_{T}} \ddot{\theta}_{O_{T}}^{-1} + 2\dot{r}_{O_{T}} \dot{\theta}_{O_{T}}^{-1} \right) Sin(\theta)_{O_{T}}^{-1} \right) + \left(\left(\tilde{r}_{T} - r_{T} \dot{\theta}_{L}^{-1} \right)^{2} Sin(\theta)_{L}^{-1} \right) + \left(\left(r_{T} \ddot{\theta}_{L}^{-1} + 2\dot{r}_{T} \dot{\theta}_{L}^{-1} \right) Cos(\theta)_{L}^{-1} \right) - \left(\left(r_{O_{T}} - r_{O_{T}} \dot{\theta}_{O_{T}}^{-1} \right) - \left(\left(r_{O_{T}} \ddot{\theta}_{O_{T}} \right) - \left(r_{O_{T}} \ddot{\theta}_{O_{T}}^{-1} \right) - \left(r_{O_{T}} \ddot{\theta}_{O_{T}}^{-1} \right) + 2\dot{r}_{O_{T}} \dot{\theta}_{O_{T}}^{-1} \right) Cos(\theta)_{D_{T}}^{-1} \right]$$

46

Again since acceleration along but not normal to the surface may exist it follows that,

$$\left\{ \left(\vec{r}_{T} - r_{T} \dot{\theta}_{L}^{-1} \right)^{2} \right\} Cos(\theta'_{L}) - \left(r_{T} \ddot{\theta}_{L}^{-1} + 2\dot{r}_{T} \dot{\theta}_{L}^{-1} \right) Sin(\theta_{L}^{-1}) + \left(\vec{r}_{o_{T'}} - r_{o_{T'}} \dot{\theta}_{o_{T'}} \right) Cos(\theta_{o_{T'}}) - \left(r_{o_{T'}} \ddot{\theta}_{o_{T'}} + 2\dot{r}_{o_{T'}} \dot{\theta}_{o_{T'}} \right) Sin(\theta_{o_{T'}}) \right\} = \dot{V}_{T}$$

$$47$$

and,

$$\left\{ (\bar{r}_{T} - r_{T} \dot{\theta}_{L})^{2} \right\} Sin(\theta'_{L}) + (r_{T} \bar{\theta}_{L}' + 2\dot{r}_{T} \dot{\theta}_{L}') Cos(\theta'_{L}) - (\bar{r}_{O_{T}} - r_{O_{T}} \dot{\theta}_{O_{T}})^{2} Sin(\theta_{O_{T}}) - (r_{O_{T}} \dot{\theta}_{O_{T}}) + 2\dot{r}_{O_{T}} \dot{\theta}_{O_{T}}) Cos(\theta_{O_{T}}) \right\} = 0$$

$$40$$

From equation 32 the derivative is,

$$-\frac{\partial \underline{r'}}{\partial t} + \frac{\partial \underline{r}}{\partial t} = \frac{\partial \underline{r}}{\partial t} = \frac{\partial \underline{r}}{\partial t}$$

.i.e. using velocity vector notation,

$$-\underline{\mathbf{V}} + \underline{\mathbf{V}}_{T} = \underline{\mathbf{V}}_{sl}$$
 50

For the attacking missile the instantaneous velocity vector \underline{V}' and acceleration vector $\underline{d}\underline{V}'/dt$ is then given by,

$$\begin{bmatrix} V' \\ \dot{V}' \end{bmatrix} = \begin{bmatrix} \dot{r}' Cos(\theta^{1}) - r' \dot{\theta}' Sin(\theta^{1}) & \dot{r}' Sin(\theta^{1}) + r' \dot{\theta} . Cos(\theta^{1}) \\ (\ddot{r}' - r' \dot{\theta}'^{2}) . Cos(\theta^{1}) - \frac{1}{r'} \frac{\partial}{\partial t} \left[r'^{2} \dot{\theta}' \right] Sin(\theta^{1}) & (\ddot{r}' - r' \dot{\theta}'^{2}) . Sin(\theta^{1}) + \frac{1}{r'} \frac{\partial}{\partial t} \left[r'^{2} \dot{\theta}' \right] Cos(\theta^{1}) \end{bmatrix} \begin{bmatrix} \dot{\underline{\iota}} \\ \dot{\underline{k}} - \end{bmatrix} + \begin{bmatrix} \underline{\nu} - \sigma_{T}' \\ \dot{\underline{\nu}} - \sigma_{T}' \end{bmatrix}$$
5

Simplifying and converting totally into earth axes unit vectors yields,

$$\underline{\underline{V}}' = \left[\left\{ \hat{r}' Cos(\theta') - r' \hat{\theta}' Sin(\theta') \right\} \left\{ \hat{r}' Sin(\theta') + r' \hat{\theta}' Cos(\theta') \right\} \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{\underline{I}}} \right] + \left[\left\{ c_{OT} \cdot Cos(\theta_{OT}^{-1}) - r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Sin(\theta_{OT}^{-1}) \right\} - \left\{ c_{OT} \cdot Sin(\theta_{OT}^{-1}) + r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) \right\} \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{\underline{I}}} \right] \\
= \left[\left\{ r' Cos(\theta') - r' \hat{\theta}' \cdot Sin(\theta') + \hat{r}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) - r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Sin(\theta_{OT}^{-1}) - r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) \right\} \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{\underline{I}}} \right] \\
= \left[\left\{ r' Cos(\theta') - r' \hat{\theta}' \cdot Sin(\theta') + \hat{r}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) - r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Sin(\theta_{OT}^{-1}) - r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) \right] \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{\underline{I}}} \right] \\
= \left[\left\{ r' Cos(\theta') - r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Cos(\theta_{OT}^{-1}) - r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) \right\} \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{\underline{I}}} \right] \\
= \left[\left\{ r' Cos(\theta') - r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Cos(\theta_{OT}^{-1}) - r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) \right\} \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{\underline{I}}} \right] \\
= \left[\left\{ r' Cos(\theta') - r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Cos(\theta_{OT}^{-1}) - r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) \right\} \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{\underline{I}}} \right] \\
= \left[\left\{ r' Cos(\theta') - r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Cos(\theta') - r' \hat{\theta}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) - r_{OT}^{-1} \cdot \hat{\theta}_{OT}^{-1} \cdot Cos(\theta_{OT}^{-1}) \right] \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{\underline{I}}} \right] \\
= \left[\left\{ r' Cos(\theta') - r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Cos(\theta') - r' \hat{\theta}_{OT}^{-1} \cdot Cos(\theta') - r' \hat{\theta}_{OT}^{-1} \cdot Cos(\theta') \right] \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{I}} \right] \\
= \left[\left\{ r' Cos(\theta') - r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Sin(\theta') + r' \hat{\theta}' \cdot Cos(\theta') - r' \hat{\theta}_{OT}^{-1} \cdot Cos(\theta') - r' \hat{\theta}_{OT}^{-1} \cdot Cos(\theta') - r' \hat{\theta}_{OT}^{-1} \cdot Cos(\theta') \right] \right] \right] \left[\underbrace{\underline{\hat{I}}}_{\underline{I}} \right]$$

and,

$$\underline{P}' = \left[\left\{ (\vec{r}' - r' \dot{\theta}'^{2}) \cdot Cos(\theta') - \frac{1}{r'} \cdot \frac{\partial}{\partial t} \left[r'^{2} \dot{\theta}' \right] Sin(\theta') + (\vec{r}_{OT}' - r_{OT}' \dot{\theta}_{OT}'^{2}) \cdot Cos(\theta_{OT}') - (r_{OT}' \ddot{\theta}_{OT}' + 2\dot{r}_{OT}' \dot{\theta}_{OT}') Sin(\theta_{OT}') \right\} \underline{I} + \left\{ (\vec{r}' - r' \dot{\theta}'^{2}) \cdot Sin(\theta') + \frac{1}{r'} \cdot \frac{\partial}{\partial t} \left[r'^{2} \dot{\theta}' \right] Cos(\theta') - (\vec{r}_{OT}' - r_{OT}' \dot{\theta}_{OT}'^{2}) \cdot Sin(\theta_{OT}') - (r_{OT}' \ddot{\theta}_{OT}' + 2\dot{r}_{OT}' \dot{\theta}_{OT}') Cos(\theta_{OT}') \right\} \underline{I} - \left[r'' - r'' \dot{\theta}' \dot{\theta}' \right] Cos(\theta') - (\vec{r}_{OT}' - r'' - r'' \dot{\theta}' - r'' \dot{\theta}' - r''' \dot{\theta}' - r'''' \dot{\theta}' - r''' \dot{\theta}' - r'''' \dot{\theta}' - r'''' \dot{\theta}' - r''' \dot{\theta}' - r'$$

23

Combining equations 43, 50 and 52 defines the instantaneous sightline angle, and subsequently sightline rate in missile body axes,

Sightline Angle and Rate

From Figure 4, the unit vector in missile body fixed axes along the sightline to the target is given by,

$$\underbrace{\begin{bmatrix} \underline{r}_{Sl} \\ \underline{sl} \end{bmatrix}}_{[\underline{r}_{T} - \underline{r}]} = \underbrace{\begin{bmatrix} (r_{T} . Cos(\theta_{L}^{1}) - r^{1} . Cos(\theta^{1})) & (-r^{1} . Sin(\theta^{1}) + r_{T} . Sin(\theta_{L}^{1})) \end{bmatrix}}_{[\underline{r}_{T} - 2r_{T} . r^{1} . Cos(\theta^{1} - \theta_{L}^{1}) + r^{1}]}^{Cos(\theta_{C} + \alpha)} \underbrace{\begin{bmatrix} \underline{t}_{B} \\ \underline{t}_{B} \end{bmatrix}}_{[\underline{r}_{T} - 2r_{T} . r^{1} . Cos(\theta^{1} - \theta_{L}^{1}) + r^{1}]}^{2}$$

$$=\frac{\left[\left(r_{T}.Cos(\theta-\theta_{L}^{'})-r'.Cos(\theta-\theta')\right) \left(r_{T}.Sin(\theta-\theta_{L}^{'})-r'.Sin(\theta-\theta')\right)\right]\left[\frac{!}{B}\right]}{\frac{k}{sl}}$$

it then follows that,

$$Cos(\gamma_{sl}) = \underline{i}_{sl} \bullet \underline{i}_{B}$$
 55

where '•' implies the vector dot product.

Whereupon,

$$Cos(\gamma_{sl}) = \frac{r_T.Cos(\theta - \theta_L^{'}) - r^{'}.Cos(\theta - \theta^{'})}{\left[r_T^{2} - 2.r_T.r^{'}.Cos(\theta^{'} - \theta_L^{'}) + r^{'}^{2}\right]^{1/2}} = \frac{r_T.Cos(\theta - \theta_L^{'}) - r^{'}.Cos(\theta - \theta^{'})}{r_{sl}}$$
56

$$Sin(\gamma_{sl}) = \frac{r_T . Sin(\theta - \theta_L^{'}) - r^{'} . Sin(\theta - \theta^{'})}{\left[r_T^{2} - 2 . r_T . r^{'} . Cos(\theta^{'} - \theta_L^{'}) + r^{'}^{2}\right]^{1/2}} = \frac{r_T . Sin(\theta - \theta_L^{'}) - r^{'} . Sin(\theta - \theta^{'})}{r_{sl}}$$
57

OI,

$$r_{sl} = Tan^{-1} \left[\frac{r_T \cdot Sin(\theta - \theta_L') - r^t \cdot Sin(\theta - \theta')}{r_T \cdot Cos(\theta - \theta_L') - r^t \cdot Cos(\theta - \theta')} \right]$$
 see Figure 5

Note here that $\theta = (\theta_c + \alpha)$ where suffix 'c' implies 'climb angle' and α is the instantaneous angle of attack. θ'_L is as defined in Figure 10 and in the limiting case at the point of impact determines, via the complement angle $(\pi/2 - \theta'_L)$, the angle the flight vector makes with the vertical at impact

Differentiating the expression for sightline angle in equation 58 yields the sightline rate as follows,

$$\hat{T} = \frac{\begin{bmatrix} r \ \dot{r}'.Cos(\theta - \alpha - \theta \ ') + r \ \dot{r}' \dot{\theta}'.Sin(\theta - \alpha - \theta \ ') - r \ \dot{\theta}' - r' \dot{r}'.Cos(\theta - \theta - \alpha) - r' \ \dot{\theta}'.Sin(\alpha - \theta + \theta ') - r' \dot{r} \ .Sin(\theta - \theta \ ') + r' \dot{r} \ \dot{\theta} \ '.Cos(\theta - \theta \ ') \end{bmatrix}}{T} + \hat{\theta}$$

$$\hat{T} = \frac{1}{T} \frac{1}{L} \frac{1}{L} \frac{1}{T} \frac{1}{L} \frac{1}{L} \frac{1}{T} \frac{1}{L} \frac{$$

$$=\frac{\left[r_{T}\dot{r}'.Sin(\theta'-\theta_{L}')+r_{T}\dot{r}'\dot{\theta}'.Cos(\theta'-\theta_{L}')-r_{T}^{2}\dot{\theta}_{L}'-r_{T}^{2}\dot{\theta}'-r_{T}^{2}\dot{r}_{T}.Sin(\theta'-\theta_{L}')+r_{T}^{2}\dot{\theta}_{L}'.Cos(\theta'-\theta_{L}')\right]}{r_{sl}}+\dot{\theta}$$

Where,

$$r_{sl}^{2} = \left[r_{T}^{2} - 2.r_{T}.r'.Cos(\theta' - \theta_{L}') + r'^{2}\right]$$
 60

Note that for instantaneous motion in a circle about o_T the substitution $\theta' = \pi/2 + \theta_{C \text{ is made}}$

Generalised Manoeuvre Conditions during the Bunt Phase

If transform the kinematic equations for the attacking missile derived are transformed and in equations 51 and 52 into trajectory axes, and if assumedconstant flight speed along the trajectory (V) with a manoeuvre g of n_g normal to the flight path,

For trajectory velocity V along the flight path,

$$-r'.\dot{\theta}' + \dot{r}_{0_{T}}'.Sin(\theta' + \theta_{0_{T}}') + r_{0_{T}}'.\dot{\theta}_{0_{T}}'.Cos(\theta' + \theta_{0_{T}}') = V$$
 61

and for zero velocity normal to the flight path,

$$-\dot{r}' - \dot{r}_{0_{T}}' \cdot Cos(\theta' \pm \theta_{0_{T}}') \pm r_{0_{T}}' \dot{\theta}_{0_{T}}' \cdot Sin(\theta' \pm \theta_{0_{T}}') = 0 - 62 - 62 - 62$$

Similarly for trajectory acceleration/manoeuvre requirements it follows that if flight speed is constant along the trajectory then acceleration is zero hence,

$$-\frac{1}{r'} \cdot \frac{\partial}{\partial t} [r'^{2} \cdot \dot{\theta}'] + (\ddot{r}_{0_{T}}' - r_{0_{T}}' \cdot \dot{\theta}_{0_{T}}'^{2}) \cdot Sin(\theta' + \theta_{0_{T}}') + \frac{1}{r_{0_{T}}'} \cdot \frac{\partial}{\partial t} [r_{0_{T}}'^{2} \cdot \dot{\theta}_{0_{T}}'] Cos(\theta' + \theta_{0_{T}}') = 0$$

$$63$$

and for manoeuvre in an instantaneous arc at constant speed the instantaneous manoeuvre g normal to the flight path velocity vector acting towards the instantaneous centre of rotation is given by,

$$-(\ddot{r}'-r'.\dot{\theta}'^{2})-(\ddot{r}_{0_{T}}'-r_{0_{T}}'.\dot{\theta}_{0_{T}}'^{2}).Cos(\theta'+\theta_{0_{T}}')+\frac{1}{r_{0_{T}}'}.\frac{\partial}{\partial t}\left[r_{0_{T}}'^{2}.\dot{\theta}_{0_{T}}'\right]Sin(\theta'+\theta_{0_{T}}')=n_{g}g$$
64

Rearranging these equations that the instantaneous velocity components for the instantaneous centre of rotation are given by,

$$\dot{r}_{0_{T}}' = (V + r'.\dot{\theta}').Sin(\theta' + \theta_{0_{T}}') - \dot{r}'.Cos(\theta' + \theta_{0_{T}}')$$

$$cos(\theta' + \theta_{0_{T}}') + \dot{r}'.Sin(\theta' + \theta_{0_{T}}')$$

and the associated instantaneous acceleration components are then defined as,

$$\ddot{r}_{0_{T}}' - r_{0_{T}}' \dot{\theta}_{0_{T}}'^{2} = \frac{1}{r'} \cdot \frac{\partial}{\partial t} \left[r'^{2} \dot{\theta}' \right] Sin(\theta' + \theta_{0_{T}}') - \left[n_{g}g + (\ddot{r}' - r' \dot{\theta}'^{2}) \right] Cos(\theta' + \theta_{0_{T}}')$$
67

$$\frac{1}{r_{0_T}} \frac{\partial}{\partial t} \left[r_{0_T}^{2} \cdot \dot{\theta}_{0_T}^{2} \right] = \frac{1}{r'} \frac{\partial}{\partial t} \left[r'^{2} \cdot \dot{\theta}' \right] Cos(\theta' + \theta_{0_T}') + \left[n_g g + (\ddot{r}' - r' \cdot \dot{\theta}'^{2}) \right] Sin(\theta' + \theta_{0_T}')$$
68

(see Figure 10)

For the target equations 44 and 45 in the matrix form,

$$\begin{bmatrix} Cos(\theta_L') & -Sin(\theta_L') \\ Sin(\theta_L') & Cos(\theta_L') \end{bmatrix} \begin{bmatrix} \dot{r}_T \\ r_T . \dot{\theta}_L \end{bmatrix} + \begin{bmatrix} Cos(\theta_{0_T}') & -Sin(\theta_{0_T}') \\ -Sin(\theta_{0_T}') & -Cos(\theta_{0_T}') \end{bmatrix} \begin{bmatrix} \dot{r}_{0_T}' \\ r_{0_T} \dot{\theta}_{0_T}' \end{bmatrix} = \begin{bmatrix} v_T \\ 0 \end{bmatrix}$$

$$69$$

which in terms of the instantaneous centre of rotation velocity components yields,

$$\begin{bmatrix} \dot{r}_{T} \\ r_{T} \cdot \dot{\theta}_{L} \end{bmatrix} = V_{T} \begin{bmatrix} \cos(\theta_{L}') \\ -\sin(\theta_{L}') \end{bmatrix} + \begin{bmatrix} -\cos(\theta_{L}' + \theta_{0_{T}}') & \sin(\theta_{L}' + \theta_{0_{T}}') \\ \sin(\theta_{L}' + \theta_{0_{T}}') & \cos(\theta_{L}' + \theta_{0_{T}}') \end{bmatrix} \begin{bmatrix} \dot{r}_{0_{T}}' \\ r_{0_{T}} \cdot \dot{\theta}_{0_{T}}' \end{bmatrix}$$

$$70$$

Similarly for the acceleration terms,

$$\begin{bmatrix} Cos(\theta_{L}') & -Sin(\theta_{L}') \\ Sin(\theta_{L}') & Cos(\theta_{L}') \end{bmatrix} \begin{bmatrix} \begin{pmatrix} \ddot{r}_{T} - r_{T} \cdot \dot{\theta}_{L} \\ \frac{1}{r_{T}} \frac{\partial}{\partial t} \begin{bmatrix} r_{T} \cdot \dot{\theta}_{L} \\ \frac{1}{r_{T}} \frac{\partial}{\partial t} \end{bmatrix} \end{bmatrix} = \begin{bmatrix} \dot{r}_{T} \\ \dot{r}_{T} \end{bmatrix}$$

which after rearranging yields

$$\begin{bmatrix} \begin{pmatrix} \ddot{r}_{T} - r_{T} \cdot \dot{\theta}_{L}^{2} \end{pmatrix} \\ \frac{1}{r_{T}} \frac{\partial}{\partial t} \begin{bmatrix} 2 \cdot \dot{\theta}_{L}^{2} \end{bmatrix} \end{bmatrix} = \dot{V}_{T} \begin{bmatrix} \cos(\theta_{L}^{2}) \\ -\sin(\theta_{L}^{2}) \end{bmatrix} + \begin{bmatrix} -\cos(\theta_{L}^{2} + \theta_{0_{T}}^{2}) & \sin(\theta_{L}^{2} + \theta_{0_{T}}^{2}) \\ \sin(\theta_{L}^{2} + \theta_{0_{T}}^{2}) & \cos(\theta_{L}^{2} + \theta_{0_{T}}^{2}) \end{bmatrix} \begin{bmatrix} \begin{pmatrix} \ddot{r}_{0_{T}} - r_{0_{T}} \cdot \dot{\theta}_{0_{T}}^{2} \\ \frac{1}{r_{0_{T}}} \frac{\partial}{\partial t} \begin{bmatrix} r_{0_{T}} - r_{0_{T}} \cdot \dot{\theta}_{0_{T}}^{2} \end{bmatrix} \end{bmatrix} \end{bmatrix}$$

$$72$$

substituting for,

$$\dot{r}_{0_{T}}$$
, $r_{0_{T}}$, $\dot{\theta}_{0_{T}}$,

to yield a relationship between the velocity and acceleration components of the attacking missile and those of the target. This yields the matrix equations,

$$\begin{bmatrix} \left(\ddot{r}_{T} - r_{T} \cdot \dot{\theta}_{L}^{2}\right) \\ \frac{1}{r_{T}} \frac{\partial}{\partial t} \begin{bmatrix} 2 \cdot \dot{\theta}_{L} \end{bmatrix} \end{bmatrix} = \dot{V}_{T} \begin{bmatrix} \cos(\theta_{L}') \\ -\sin(\theta_{L}') \end{bmatrix} + \begin{bmatrix} \cos(\theta' - \theta_{L}') & -\sin(\theta' - \theta_{L}') \\ \sin(\theta' - \theta_{L}') & \cos(\theta' - \theta_{L}') \end{bmatrix} \begin{bmatrix} n_{g}g + (\ddot{r}' - r'\dot{\theta}'^{2}) \\ \frac{1}{r'} \frac{\partial}{\partial t} [r'^{2} \cdot \dot{\theta}'] \end{bmatrix}$$

$$74$$

$$\begin{bmatrix} \dot{r}_{T} \\ r_{T} . \dot{\theta}_{L} \end{bmatrix} = V_{T} \begin{bmatrix} Cos(\theta_{L}') \\ -Sin(\theta_{L}') \end{bmatrix} + \begin{bmatrix} -Sin(\theta' - \theta_{L}') & Cos(\theta' - \theta_{L}') \\ Cos(\theta' - \theta_{L}') & Sin(\theta' - \theta_{L}') \end{bmatrix} \begin{bmatrix} (V + r'\dot{\theta}') \\ \dot{r}' \end{bmatrix}$$
75

From equations 58 and 60 the instantaneous radii are derived from the instantaneous centre of rotation to the attacking missile (r') and the target (r_T) as follows,

$$r' = \frac{Sin(\gamma_{sl} - \theta_c - \alpha + \theta'_L)}{Cos(\theta_c - \theta'_L)}.r_{sl}$$
 76

$$r_T = \frac{Cos(\gamma_{sl} - \alpha)}{Cos(\theta_c - \theta'_L)} r_{sl}$$
 77

and from equation 75,

$$\dot{r}_T = V_T Cos(\theta_L) - (V + r'.\dot{\theta}_C).Cos(\theta_C - \theta_L') - \dot{r}'.Sin(\theta_C - \theta_L')$$
 78

Differentiating the equation for r' in equation 76 above results in the following expression;

$$\dot{r}^{\prime}Cos(\theta_{c} - \theta^{\prime}_{L}) = \frac{\left(\left(-\dot{\theta}_{c} + \dot{\theta}^{\prime}_{L}\right)r_{sl} \cdot Cos(\gamma_{sl} - \alpha)\right)}{Cos(\theta^{\prime} - \theta^{\prime}_{L})}$$

$$+ \dot{\gamma}_{sl} \cdot r_{sl} \cdot Cos(\gamma_{sl} - \theta_{c} - \alpha + \theta^{\prime}_{L})$$

$$+ \dot{r}_{sl} \cdot Sin(\gamma_{sl} - \theta_{c} - \alpha + \theta^{\prime}_{L})$$

$$- \dot{\alpha} \cdot r_{sl} \cdot Cos(\gamma_{sl} - \theta_{c} - \alpha + \theta^{\prime})$$
79

Substituting for,

$$r'$$
, \dot{r}' , r_T , \dot{r}_T

in the equation for \dot{r}_{sl} (equation 59) and rearranging then yields,

$$\dot{\theta}_{c} = \left(\dot{\gamma}_{sl} - \dot{\alpha}\right) - \frac{\left(\frac{\dot{r}_{sl}}{r_{sl}}\right)}{Tan\left(\gamma_{sl} - \alpha - \theta_{c} + \theta_{L}'\right)} - \left(\frac{V.Cos(\theta_{c} - \theta_{L}') - V_{T}.Cos(\theta_{L}')}{r_{sl}.Sin(\gamma_{sl} - \alpha - \theta_{c} + \theta_{L}')}\right)$$
81

If we now consider instantaneous motion in an arc of a circle, the number of g's pulled (n_g) is directly related to the flight path rate $\dot{\theta}_c$ and the speed (here considered to be a constant V) by the expression,

$$n_{g}g = -\dot{\theta}_{c}.V$$
 82

It therefore follows that the demand g to achieve intercept with a moving target is instantaneously given by the expression,

$$n_{\mathcal{E}} = -\left(\frac{v}{g}\right) \left[\dot{\gamma}_{sl} - \dot{\alpha} - \frac{\left(\frac{\dot{r}_{sl}}{r_{sl}}\right)}{Tan(\gamma_{sl} - \alpha - \theta_c + \theta_L')} - \left(\frac{v.Cos(\theta_c - \theta_L') - v_T.Cos(\theta_L')}{r_{sl}.Sin(\gamma_{sl} - \alpha - \theta_c + \theta_L')}\right)\right]$$
83

At each point of the final bunt trajectory, the missile rotates about the instantaneous centre of rotation and that the instantaneous radius from this centre to the missile is equal to that radius from the centre to the target, then $r' = r_T$ from above. This is in keeping with our outline philosophy given in section 2. As a result $R = r' = r_T$ from which assumption it follows that,

$$R = \frac{Sin(\gamma_{sl} - \theta_c - \alpha + \theta_L^{\dagger})}{Cos(\theta_c - \theta_L^{\dagger})} r_{sl} = \frac{Cos(\gamma_{sl} - \alpha)}{Cos(\theta_c - \theta_L^{\dagger})} r_{sl}$$

From equation 84 it then follows that,

$$Sin(\gamma_{sl} - \theta_c - \alpha + \theta_L^*) = Cos(\gamma_{sl} - \alpha)$$
 85

Solving this equation then yields the solution for θ_L , as

$$\theta'_{L} = \frac{\pi}{2} \pm (\gamma_{sl} - \alpha) - \gamma_{sl} + \theta_{c} + \alpha \qquad . \qquad 86$$

Note there are two possible solutions,

$$\theta'_{L1} = \frac{\pi}{2} + \theta_c$$
, $\theta'_{L2} = \frac{\pi}{2} + \theta_c - 2.(\gamma_{sl} - \alpha)$ 87

Of these two solutions, solution 1 refers to the condition for the radius vector from the instantaneous centre of rotation to the target at the point of impact and solution 2 is the arbitrary case for the missile in flight during the bunt. It should be noted in this case that despite assuming (for the purposes of the algorithm) that the two radii are instantaneously of the same length, they are allowed to vary in length at the same rate throughout the bunt trajectory.

In keeping with the generalised analysis, only the second solution will be considered from here. Thus substituting for solution 2 in the expression for R it follows that,

$$\alpha = \gamma_{sl} - Sin^{-1} \left(\frac{r_{sl}}{2R} \right)$$
 88

and for the manoeuvre g,

$$n_{g} = -\left(\frac{V}{g}\right)\left[\left(\dot{\gamma}_{sl} - \dot{\alpha}\right) - \left(\frac{\dot{r}_{sl}}{r_{sl}}\right)Tan\left(\gamma_{sl} - \alpha\right) - \left(\frac{V.Sin(2.(\gamma_{sl} - \alpha)) - V_{T}.Sin(\theta_{c} - 2.(\gamma_{sl} - \alpha))}{r_{sl}.Cos(\gamma_{sl} - \alpha)}\right)\right]$$
89

Also since we are concerned with instantaneous motion in an arc of a circle at constant speed V, it follows that,

$$V = -\dot{\theta}_c.R \qquad 90$$

Substituting for R then yields,

$$\alpha = \gamma_{sl} + Sin^{-1} \left(\frac{r_{sl} . \dot{\theta}_c}{2V} \right)$$
 91

It follows from equation 91 that as $r_{sl} \mapsto 0$, so $\alpha \mapsto \gamma_{sl}$ and therefore if in particular $\gamma_{sl} \mapsto 0$ so $\alpha \mapsto 0$. Further since \dot{e}_c is related to the manoeuvre g demand to hit the target, it follows that a direct link exists to the associated incidence at impact. In summary therefore a terminal engagement algorithm which ties manoeuvre g to climb rate and sightline look angle enables the impact grazing angle to be determined (subject to tight autopilot control). Throughout the bunt, the sightline needs to maintain look angle on the target and to maintain the associated g to manoeuvre to impact translates into an associated incidence demand. If this incidence is within stall limits of all lifting surfaces while maintaining the required manoeuvre g to achieve the bunt trajectory them the terminal engagement algorithm will comply with all requirements to fly the bunt trajectory and impact the target.

In varying the incidence in this way to accommodate a manoeuvre g while maintaining sightline look on the target, it is essential that the wing-tail interlinked gearing is continually adjusted. This will leave the residual tail control to remove any body rate transients and correct for any minor errors in achieving the required impact conditions resulting from autopilot /systems lags either inherent or resulting from atmospheric disturbance.

It should be noted in equation 89 the velocity of the target V_T is the instantaneous velocity of the target at the point of breakaway into the bunt and the value of manoeuvre g calculated n_g is that manoeuvre g which at that instant is required to describe an arc which intercepts the target at that point. However since the target continues to move, we need to apply a specific shape function for the trajectory post breakaway from the climb phase into the bunt which addresses the subsequent manoeuvre to intercept.

Specific Application of The Generic Terminal Engagement Algorithm

Assume the instantaneous centre of rotation of the radial vector to the attacking missile as acting along the extended pull-up radial vector assumed set at an angle θ^*_{cp} equal to that angle at which breakaway takes place between the pull up, and the bunt manoeuvre. In application this may be translated into a specific sightline range which is more practical in a real world application. For now retain this convention for analytical purposes.

It follows then that,

$$\underline{\underline{V}}_{o_{\underline{T}}}' = \dot{r}^* \underline{\underline{k}}_{traj}^*$$
 92

and,

$$\underline{\mathbf{v}}_{O_{T}} = \begin{bmatrix} \dot{r}_{O_{T}}, & r_{O_{T}} \cdot \dot{\theta}_{O_{T}} \end{bmatrix} \begin{bmatrix} \dot{t}_{O_{T}}, \\ \dot{\underline{k}}_{O_{T}} \end{bmatrix}$$

Transforming into trajectory axes,

$$\underline{\underline{V}}_{O_{T}} = \begin{bmatrix} \dot{r}_{O_{T}} & r_{O_{T}} & \dot{\theta}_{O_{T}} \\ \dot{r}_{O_{T}} & \dot{r}_{O_{T}} & \dot{\theta}_{O_{T}} \end{bmatrix} \begin{bmatrix} Cos(\theta_{O_{T}}) & -Sin(\theta_{O_{T}}) \\ -Sin(\theta_{O_{T}}) & -Cos(\theta_{O_{T}}) \end{bmatrix} \begin{bmatrix} Cos(\theta *_{c}) & Sin(\theta *_{c}) \\ Sin(\theta *_{c}) & -Cos(\theta *_{c}) \end{bmatrix} \begin{bmatrix} \underline{i}_{traj} *_{traj} *_{traj} *_{traj} *_{traj} *_{traj} *_{traj} \end{bmatrix}$$

$$94$$

Rearranging equations 92, 93 and 94 then yields,

$$\begin{bmatrix} \dot{r}_{0_T} \\ r_{0_T} \cdot .\dot{\theta}_{0_T} \end{bmatrix} = \begin{bmatrix} \cos(\theta_{0_T} + \theta_c^*) & \sin(\theta_{0_T} + \theta_c^*) \\ -\sin(\theta_{0_T} + \theta_c^*) & \cos(\theta_{0_T} + \theta_c^*) \end{bmatrix} \begin{bmatrix} 0 \\ \dot{r}^*_{cp} \end{bmatrix}$$
95

But it can be shown that,

$$\begin{bmatrix} \dot{r}_{T} \\ r_{T} \cdot \dot{\theta}'_{L} \end{bmatrix} = V_{T} \begin{bmatrix} \cos(\theta_{L}') \\ -\sin(\theta_{L}') \end{bmatrix} + \begin{bmatrix} -\cos(\theta_{L}' + \theta_{0_{T}}') & \sin(\theta_{L}' + \theta_{0_{T}}') \\ \sin(\theta_{L}' + \theta_{0_{T}}') & \cos(\theta_{L}' + \theta_{0_{T}}') \end{bmatrix} \begin{bmatrix} \dot{r}_{0_{T}}' \\ r_{0_{T}} \cdot \dot{\theta}_{0_{T}}' \end{bmatrix}$$
96

Substituting this expression in equation 70 yields,

$$\begin{bmatrix} \dot{r}_{T} \\ r_{T} \cdot \dot{\theta}'_{L} \end{bmatrix} = V_{T} \cdot \begin{bmatrix} Cos(\theta_{L}') \\ -Sin(\theta_{L}') \end{bmatrix} + \begin{bmatrix} -Cos(\theta *_{c} - \theta'_{L}) & -Sin(\theta *_{c} - \theta'_{L}) \\ -Sin(\theta *_{c} - \theta'_{L}) & Cos(\theta *_{c} - \theta'_{L}) \end{bmatrix} \begin{bmatrix} 0 \\ \dot{r} *_{cp} \end{bmatrix}$$
97

From equation 75 now repeated here for ease of reference,

$$\begin{bmatrix} \dot{r}_{T} \\ r_{T} . \dot{\theta}_{L} \end{bmatrix} = V_{T} \begin{bmatrix} Cos(\theta_{L}') \\ -Sin(\theta_{L}') \end{bmatrix} + \begin{bmatrix} -Sin(\theta' - \theta_{L}') & Cos(\theta' - \theta_{L}') \\ Cos(\theta' - \theta_{L}') & Sin(\theta' - \theta_{L}') \end{bmatrix} \begin{bmatrix} (V + r'\dot{\theta}') \\ \dot{r}' \end{bmatrix}$$
98

Equating equations 97 and 98 and rearranging yields the relationship,

$$\begin{bmatrix} V + r'\dot{\theta}' \\ \dot{r}' \end{bmatrix} = \begin{bmatrix} -Sin(\theta *_{c} - \theta') & Cos(\theta *_{c} - \theta') \\ -Cos(\theta *_{c} - \theta') & -Sin(\theta *_{c} - \theta') \end{bmatrix} \begin{bmatrix} 0 \\ \dot{r} *_{cp} \end{bmatrix}$$
99

It is assumed that at any instant in time,

$$R = r^{\scriptscriptstyle 1} = r_{\scriptscriptstyle T} \qquad , \qquad \dot{R} = \dot{r}^{\scriptscriptstyle 1} = \dot{r}_{\scriptscriptstyle T} \qquad 100$$

In this assumption, the rate of change of radius is none zero.

$$\dot{R} = V_T . Cos(\theta_L') - \dot{r} *_{cp} . Sin(\theta *_c - \theta_L') = -Sin(\theta *_c - \theta') \dot{r} *_{cp}$$
 101

Hence,

$$\hat{R} = \frac{-V_T.Sin(\theta *_c - \theta^1).Cos(\theta_L^1)}{\left[Sin(\theta *_c - \theta_L^1) - Sin(\theta *_c - \theta^1)\right]}$$
102

Motion in an instantaneous arc of a circle during the bunt phase results in the following equation,

$$R = \left(\frac{r_{sl}}{2.Sin(\gamma_{sl} - \alpha)}\right)$$
 103

Differentiating then yields,

$$\frac{\dot{R}}{R} = \frac{\dot{r}_{sl}}{r_{sl}} - \frac{\left(\dot{\gamma}_{sl} - \dot{\alpha}\right)}{Tan\left(\gamma_{sl} - \alpha\right)}$$
104

Substituting for equations 102, 103 and utilising the general solution for θ_L ' = $\pi/2+\theta c-2(\gamma sl-\alpha)$ and the substitution for $\theta'=\pi/2+\theta c$,

$$\frac{\dot{R}}{R} = \frac{\dot{r}_{sl}}{r_{sl}} - \frac{\left(\dot{\gamma}_{sl} - \dot{\alpha}\right)}{Tan\left(\gamma_{sl} - \alpha\right)} = -\frac{2.V_T.Sin\left(\gamma_{sl} - \alpha\right).Cos\left(\theta_c - \theta_c *\right).Sin\left(\theta_c - 2.\left(\gamma_{sl} - \alpha\right)\right)}{r_{sl}.\left[Cos\left(\theta_c - \theta_c *\right) - Cos\left(\left(\theta_c - \theta_c *\right) - 2.\left(\gamma_{sl} - \alpha\right)\right)\right]}$$
105

Whereupon the final version of the terminal engagement algorithm becomes

$$ng = \left(\frac{v}{g}\right)\left[\frac{-2.V_T.Sin(\gamma_{sl} - \alpha)Tan(\gamma_{sl} - \alpha)Cos(\theta_c - \theta_c *).Sin(\theta_c - 2.(\gamma_{sl} - \alpha))}{r_{sl}.\left[Cos(\theta_c - \theta_c *) - Cos((\theta_c - \theta_c *) - 2.(\gamma_{sl} - \alpha))\right]} + \left(\frac{v.Sin(2.(\gamma_{sl} - \alpha)) - V_T.Sin(\theta_c - 2.(\gamma_{sl} - \alpha))}{r_{sl}.Cos(\gamma_{sl} - \alpha)}\right)\right]$$

Note here that θ^*_c relates to the climb angle into pull-up at which breakaway occurs into the bunt.

Rearranging this equation to be in the form,

$$= \left(\frac{V}{g.r.}\right) \left[\frac{-2V_T.Sin(\gamma_{sl} - \alpha)Tan(\gamma_{sl} - \alpha)Cos((\theta - \alpha) - (\theta^* - \alpha^*))Sin((\theta - \alpha) - 2.(\gamma_{sl} - \alpha))}{\left[Cos((\theta - \alpha) - (\theta^* - \alpha^*)) - Cos(((\theta - \alpha) - (\theta^* - \alpha^*)) - 2.(\gamma_{sl} - \alpha))\right]} + \left(\frac{V.Sin(2.(\gamma_{sl} - \alpha)) - V_T.Sin((\theta - \alpha) - 2.(\gamma_{sl} - \alpha))}{Cos(\gamma_{sl} - \alpha)}\right)\right] 107$$

At any point in the trajectory, control to achieve an implied $\alpha = \alpha_0$ (i.e. appropriate ZLL) since the sightline angle γ_{sl} minus this angle is constant at the same point, it opens the possibility of varying a demand ZLL to achieve a favourable look angle to the target while ensuring manoeuvre potential below the stall. Note here that the ZLL is implied to act along the flight velocity vector. The remaining terms in the expression which concern body attitude can be derived by integration of body rate from rate gyros via the autopilot. Terms marked with an 'asterisk' concern conditions at breakaway from the pull-up manoeuvre when entering the bunt phase. These may be identified at a specific sightline range to target intercept. These features are expressed graphically in Figure 13.

TRANSFORMATION MATRICES

In defining the algorithm, use is made of several axes sets as defined in Figure 10. For convenience, axes transformations between these sets needed in the analysis are summarised below.

Transformation of axes i_{traj} , k_{traj} to i_B , k_B and visa versa through angular rotation α (angle of attack).

$$\begin{bmatrix} \underline{i}_{traj} \\ \underline{k}_{traj} \end{bmatrix} = \begin{bmatrix} Cos(\alpha) & Sin(\alpha) \\ -Sin(\alpha) & Cos(\alpha) \end{bmatrix} \begin{bmatrix} \underline{i}_{B} \\ \underline{k}_{B} \end{bmatrix} , \begin{bmatrix} \underline{i}_{B} \\ \underline{k}_{B} \end{bmatrix} = \begin{bmatrix} Cos(\alpha) & -Sin(\alpha) \\ \underline{k}_{B} \end{bmatrix} \begin{bmatrix} \underline{i}_{traj} \\ Sin(\alpha) & Cos(\alpha) \end{bmatrix} \begin{bmatrix} \underline{i}_{traj} \\ \underline{k}_{traj} \end{bmatrix}$$
108

Transformation of axes \underline{i}_{traj} , \underline{k}_{traj} to \underline{i} , \underline{k} and visa versa through angular rotation θ '.

$$\begin{bmatrix} \underline{i}_{traj} \\ \underline{k}_{traj} \end{bmatrix} = \begin{bmatrix} Sin(\theta^{1}) & -Cos(\theta^{1}) \\ -Cos(\theta^{1}) & -Sin(\theta^{1}) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} , \quad \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} = \begin{bmatrix} Sin(\theta^{1}) & -Cos(\theta^{1}) \\ -Cos(\theta^{1}) & -Sin(\theta^{1}) \end{bmatrix} \begin{bmatrix} \underline{i}_{traj} \\ \underline{k}_{traj} \end{bmatrix}$$
109

Transformation of axes \underline{i} , \underline{k} to \underline{i}_1 , \underline{k}_1 and visa versa through angular rotation θ_1 .

$$\begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} = \begin{bmatrix} Cos(\theta) & Sin(\theta_1) \\ Sin(\theta_1) & -Cos(\theta) \end{bmatrix} \begin{bmatrix} \underline{i}_1 \\ \underline{k}_1 \end{bmatrix} , \begin{bmatrix} \underline{i}_1 \\ \underline{k}_1 \end{bmatrix} = \begin{bmatrix} Cos(\theta) & Sin(\theta_1) \\ Sin(\theta_1) & -Cos(\theta) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix}$$
 110

Transformation of axes i, \underline{k} to \underline{i}_{traj} , \underline{k}_{traj} and visa versa through angular rotation θ_c .

$$\begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} = \begin{bmatrix} Cos(\theta_c) & Sin(\theta_c) \\ Sin(\theta_c) & -Cos(\theta_c) \end{bmatrix} \begin{bmatrix} \underline{i}_{traj} \\ \underline{k}_{traj} \end{bmatrix} , \begin{bmatrix} \underline{i}_{traj} \\ \underline{k}_{traj} \end{bmatrix} = \begin{bmatrix} Cos(\theta_c) & Sin(\theta_c) \\ Sin(\theta_c) & -Cos(\theta_c) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix}$$
111

Transformation of axes \underline{i} , \underline{k} to \underline{i}_T , \underline{k}_T and visa versa through angular rotation θ'_L .

$$\begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} = \begin{bmatrix} Cos(\theta_L) & Sin(\theta_L) \\ Sin(\theta_L) & -Cos(\theta_L) \end{bmatrix} \begin{bmatrix} \underline{i}_T \\ \underline{k}_T \end{bmatrix} , \begin{bmatrix} \underline{i}_T \\ \underline{k}_T \end{bmatrix} = \begin{bmatrix} Cos(\theta_L) & Sin(\theta_L) \\ Sin(\theta_L) & -Cos(\theta_L) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix}$$
112

Transformation of axes i, <u>k</u> to $i_{OT'}$, $k_{OT'}$ and visa versa through angular rotation $\theta_{OT'}$.

$$\begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix} = \begin{bmatrix} \cos(\theta_{O_T}) & -\sin(\theta_{O_T}) \\ -\sin(\theta_{O_T}) & -\cos(\theta_{O_T}) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \\ OT \end{bmatrix} , \quad \begin{bmatrix} \underline{i} \\ \underline{k} \\ OT \end{bmatrix} = \begin{bmatrix} \cos(\theta_{O_T}) & -\sin(\theta_{O_T}) \\ -\sin(\theta_{O_T}) & -\cos(\theta_{O_T}) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix}$$
113

Transformation of axes i, k to i_{ep}, k_{ep} and visa versa through angular rotation θ_{ep} .

$$\begin{bmatrix} \underline{i} \\ - \end{bmatrix} = \begin{bmatrix} Sin(\theta_{cp}) & Cos(\theta_{cp}) \\ - Cos(\theta_{cp}) & Sin(\theta_{cp}) \end{bmatrix} \begin{bmatrix} \underline{i}_{cp} \\ \underline{k}_{cp} \end{bmatrix} , \begin{bmatrix} \underline{i}_{cp} \\ \underline{k}_{cp} \end{bmatrix} = \begin{bmatrix} Sin(\theta_{cp}) & -Cos(\theta_{cp}) \\ Cos(\theta_{cp}) & Sin(\theta_{cp}) \end{bmatrix} \begin{bmatrix} \underline{i} \\ \underline{k} \end{bmatrix}$$
114

•

Transformation of axes $(\underline{i}_{traj}, \underline{k}_{traj})$ to $(\underline{i}', \underline{k}')$ and visa versa.

$$\begin{bmatrix} \underline{i'} \\ \underline{k'} \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \underline{i} traj \\ \underline{k} traj \end{bmatrix} , \begin{bmatrix} \underline{i} traj \\ \underline{k} traj \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} \underline{i'} \\ \underline{k'} \end{bmatrix}$$
 113

CLAIMS

- 1. Control system for craft having a main wing control surface and a secondary wing control surface, the system comprising synchronised operation of the main wing control surface and the secondary wing control surface.
- 2. Control system for craft having a main wing control surface and a secondary wing control surface, the system comprising linking means for synchronised operation of the main wing control surface and the secondary wing control surface.
- 3. A system according to Claim 1 or 2 wherein synchronised operation provides identical rotational and/or translational movement of the main and secondary control surfaces.
- 4. A system according to any preceding claim wherein synchronised operation provides proportional rotational and/or translational movement of the main and secondary control surfaces.
- 5. A system according to any preceding claim wherein synchronised operation provides geared rotational and/or translational movement of the main and secondary control surfaces.
- 6. A system according to any preceding claim wherein synchronised operation provides variable rotational and/or translational movement of the main and secondary control surfaces.

- 7. A system according to any preceding claim wherein the craft comprises more than one main wing control surface and/or more than one secondary wing control surface.
- 8. A system according to any preceding claim wherein substantially all the control surface of the main wing and/or the secondary wing is moveable under the synchronised operation.
- 9. A system according to any preceding claim wherein a flap portion of the main wing control surface is moveable under the synchronised operation.
- 10. A system according to any preceding claim wherein the craft comprises an aircraft.
- 11. A system according to any preceding claim wherein the craft comprises a marine craft.
- 12. A system according to any of Claims 10 or 11 wherein the craft comprises a missile.
- 13. A system according to any of Claims 11 or 12 wherein the craft comprises a torpedo.
- 14. A system according to any Claims 12 or 13 wherein the craft is unmanned.
- 15. A system according to any preceding claim comprising means to off-set the body axis relative to the instantaneous flight path velocity vector.

- 16. A system according to any preceding claim comprising means to effect an applied manoeuvre about an instantaneous zero lift line.
- 17. A system according to any preceding claim comprising means to maintain constant speed V.
- 18. A system according to any preceding claim comprising means to adjust, at predetermined time intervals, the control surfaces setting to effect configuration of the zero lift line manoeuvre.
- 19. A system according to any preceding claim having a controller to provide, selectively as required:-

constant speed;

variable speed;

proportional rotational and/or translation movement of control surfaces; geared rotational and/or translational movement of control surfaces; variable rotational and/or translational movement of control surfaces.

- 20. A craft having a control system according to any one or more of Claims 1 to 19.
- 21. A method of controlling a craft having a main wing control surface and a secondary wing control surface, the method comprising synchronising operation of the main wing control surface and the secondary wing control surface.
- 22. A method of controlling a craft having a main wing control surface and a secondary wing control surface, the method comprising operating linking means to synchronise operation of the main wing control surface and the secondary wing control surface.

- 23. A method according to Claim 21 or 22 comprising providing identical rotational and/or translational movement of the main and secondary control surfaces.
- 24. A method according to any of Claims 21 to 23 comprising providing proportional rotational and/or translational movement of the main and secondary control surfaces.
- 25. A method according to any of Claims 21 to 24 comprising providing geared rotational and/or translational movement of the main and secondary control surfaces.
- 26. A method according to any of Claims 21 to 25 comprising providing varied rotational and/or translational movement of the main and secondary control surfaces.
- 27. A method according to any of Claims 21 to 26 comprising moving more than one main wing control surface and/or more than one secondary wing control surface under the synchronised operation.
- 28. A method according to any of Claims 21 to 27 comprising moving substantially all the control surface of the main wing and/or the secondary wing under the synchronised operation.
- 29. A method according to any of Claims 21 to 27 comprising moving a flap portion of the main wing control surface and/or of the secondary wing control surface under the synchronised operation.

- 30. A method according to any of Claims 21 to 28 wherein the craft comprises an aircraft, or a marine craft, or a missile, or a torpedo.
- 31. A method according to any of Claims 21 to 30 comprising off-setting the body axis relative to the instantaneous flight path velocity vector.
- 32. A method according to any of Claims 21 to 31 comprising effecting an applied manoeuvre about an instantaneous zero lift line.
- 33. A method according to any of Claims 21 to 32 comprising maintaining constant speed V.
- 34. A method according to any of Claims 21 to 33 comprising adjusting, at predetermined time intervals, the control surfaces settings to effect configuration of the zero lift line manoeuvre.
- 35. A method according to any of Claims 21 to 34 comprising controlling, selectively as required, to provide:-

constant speed;

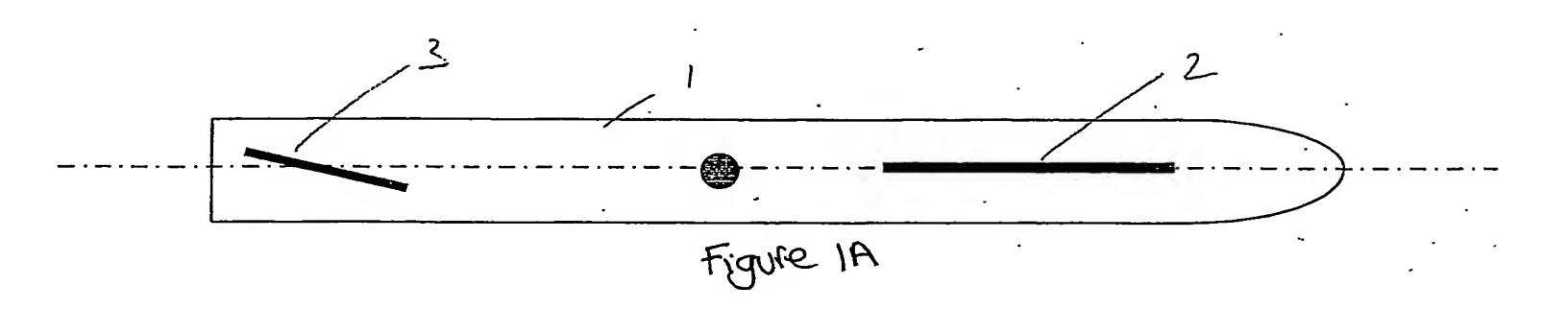
variable speed;

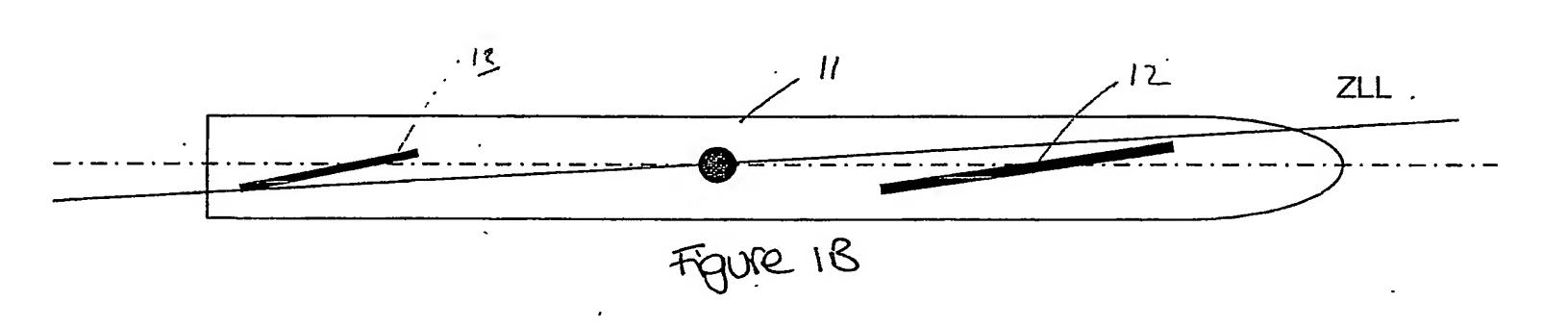
proportional rotational and/or translational movement of control surfaces;

geared rotational and/or translational movement of control surfaces; variable rotational and/or translational movement of control surfaces.

36. A computer program product directly loadable into the internal memory of a digital computer, comprising software code portions for performing the method any one or more of Claims 21 to 35 when said product is run on a computer.

- 37. A computer program directly loadable into the internal memory of a digital computer, comprising software code portions for performing the method any one or more of Claims 21 to 35 when said program is run on a computer.
- 38. A carrier, which may comprise electronic signals, for a computer program of Claim 37.
- 39. Electronic distribution of a computer program product of Claim 36 or a computer program of Claim 37 or a carrier of Claim 38.
- 40. Control system for a craft, the system substantially as hereinbefore described with reference to and/or as illustrated in, any one or more of Figures 1B to 6B, 7 and 9 of the accompanying drawings.
- Method of operating a control system substantially as hereinbefore described with reference to, and/or as illustrated in, any one or more of Figures 1B to 6B, 7 and 9 of the accompanying drawings.





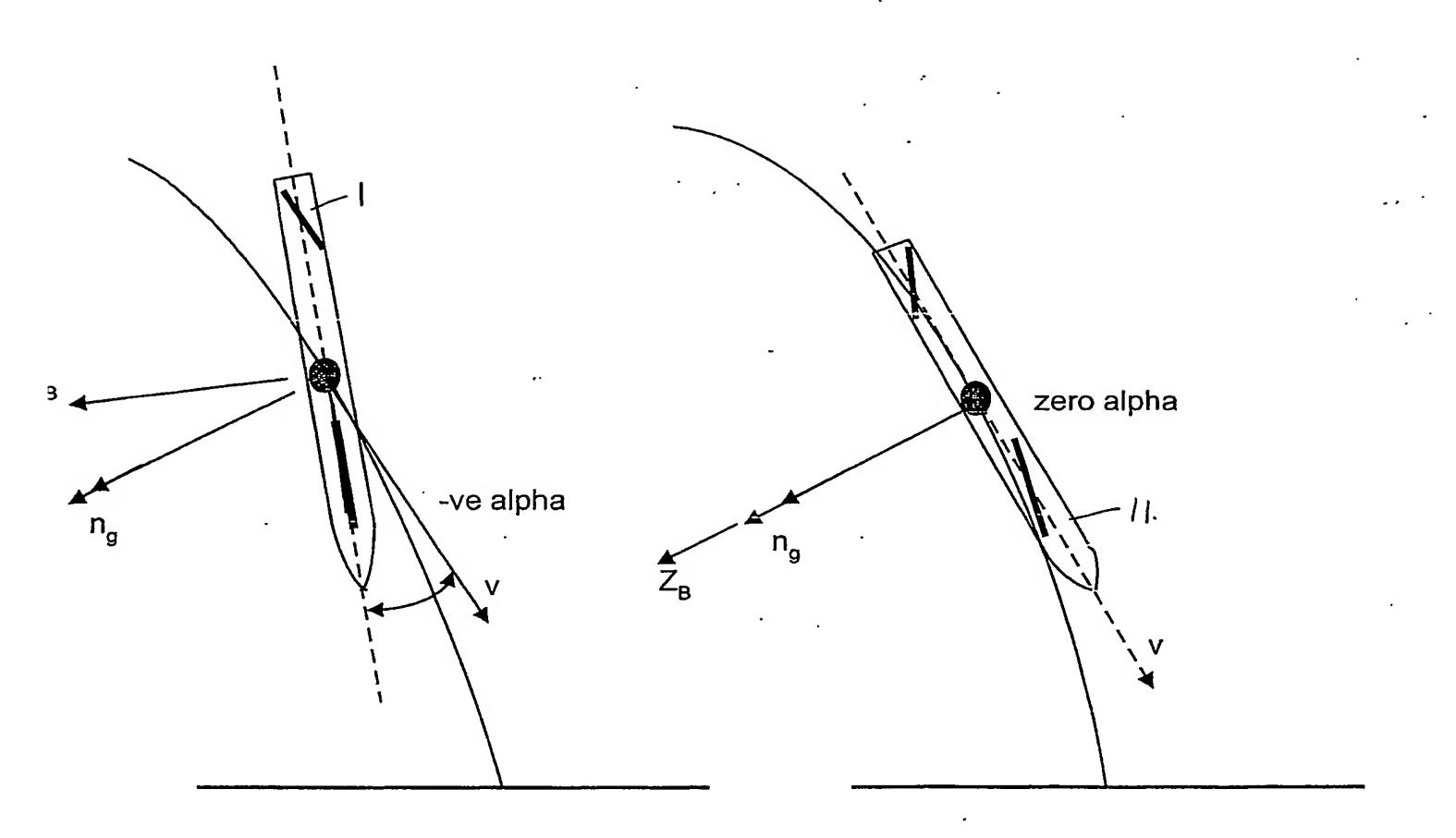
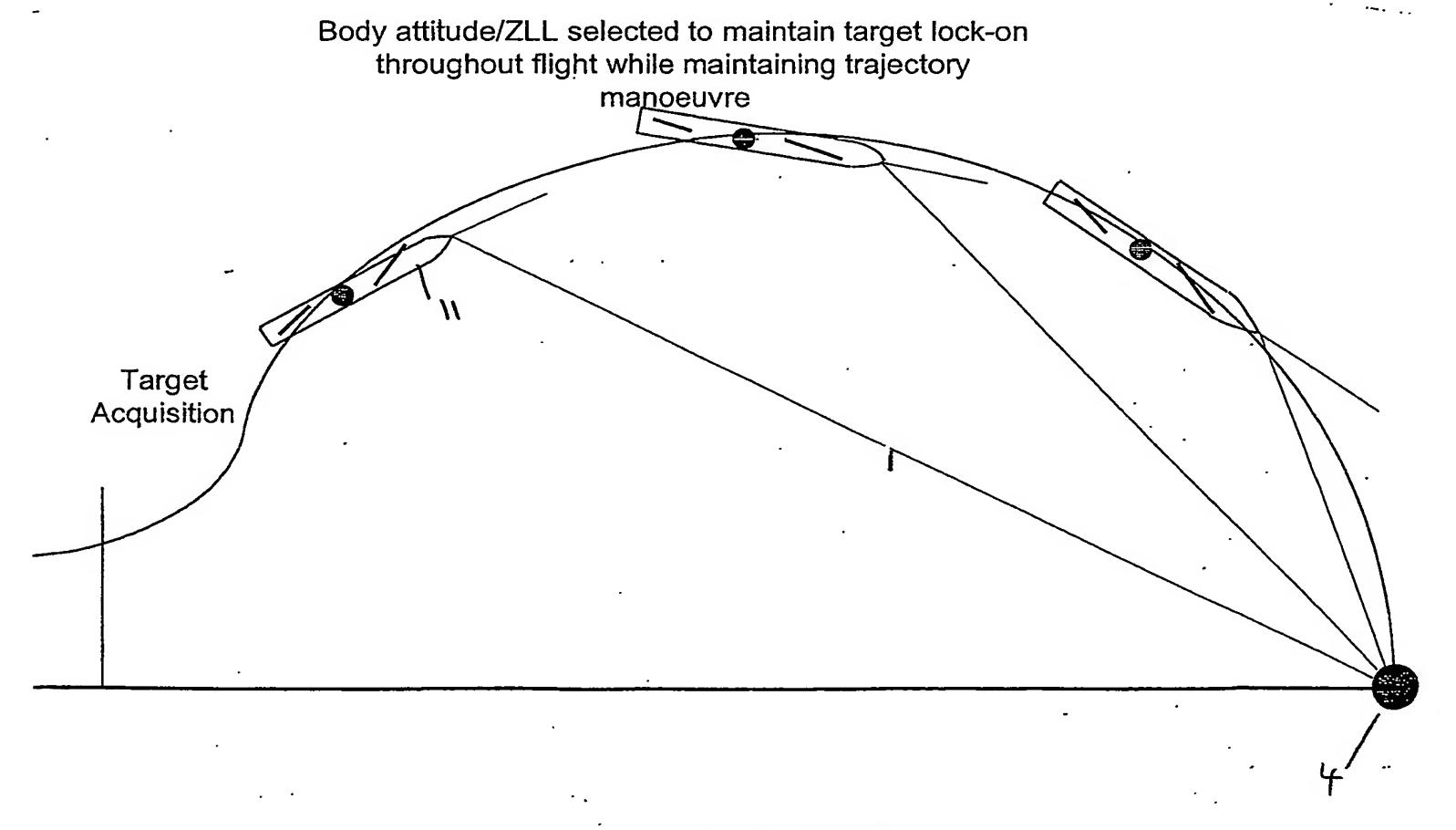
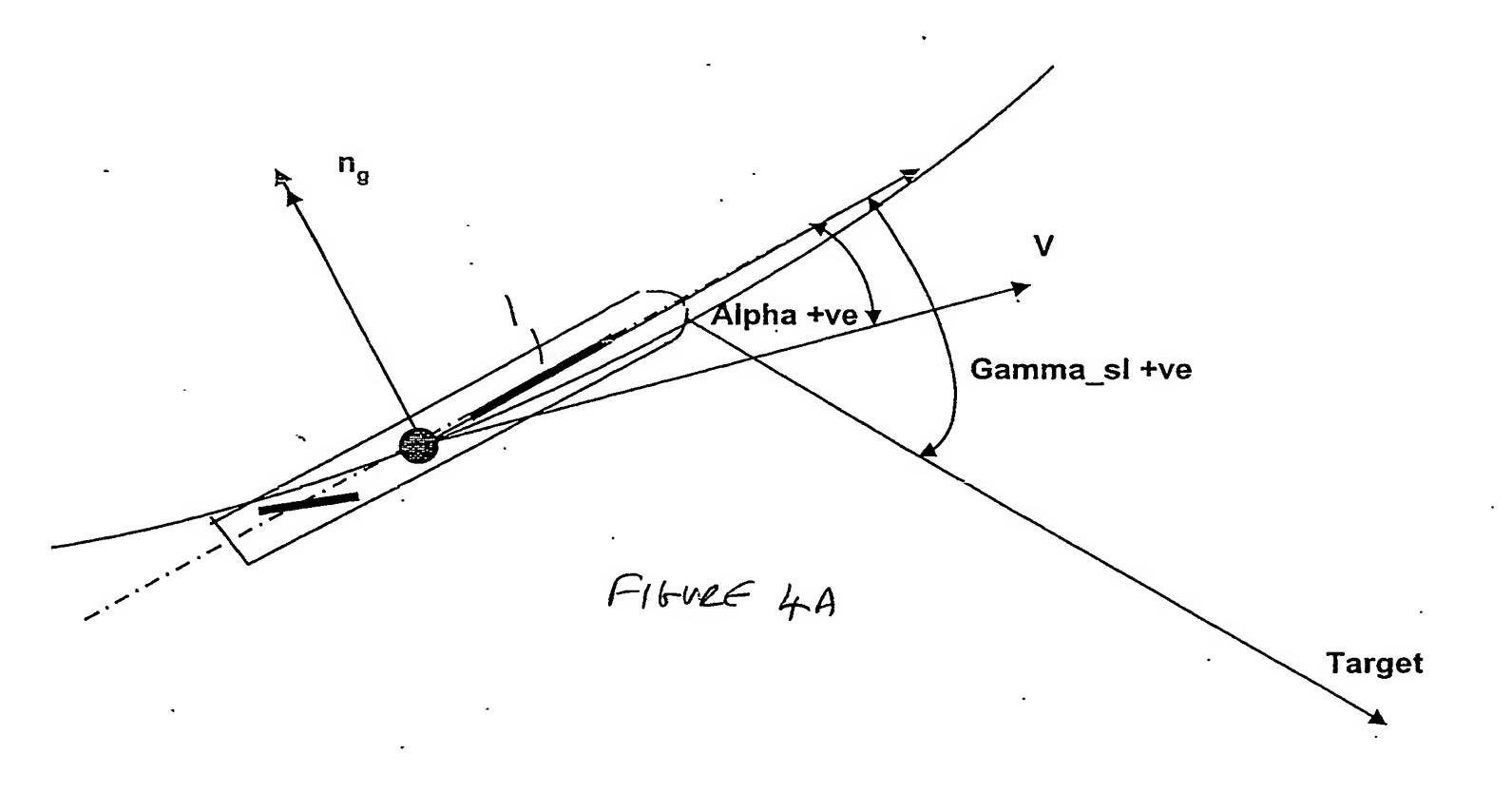


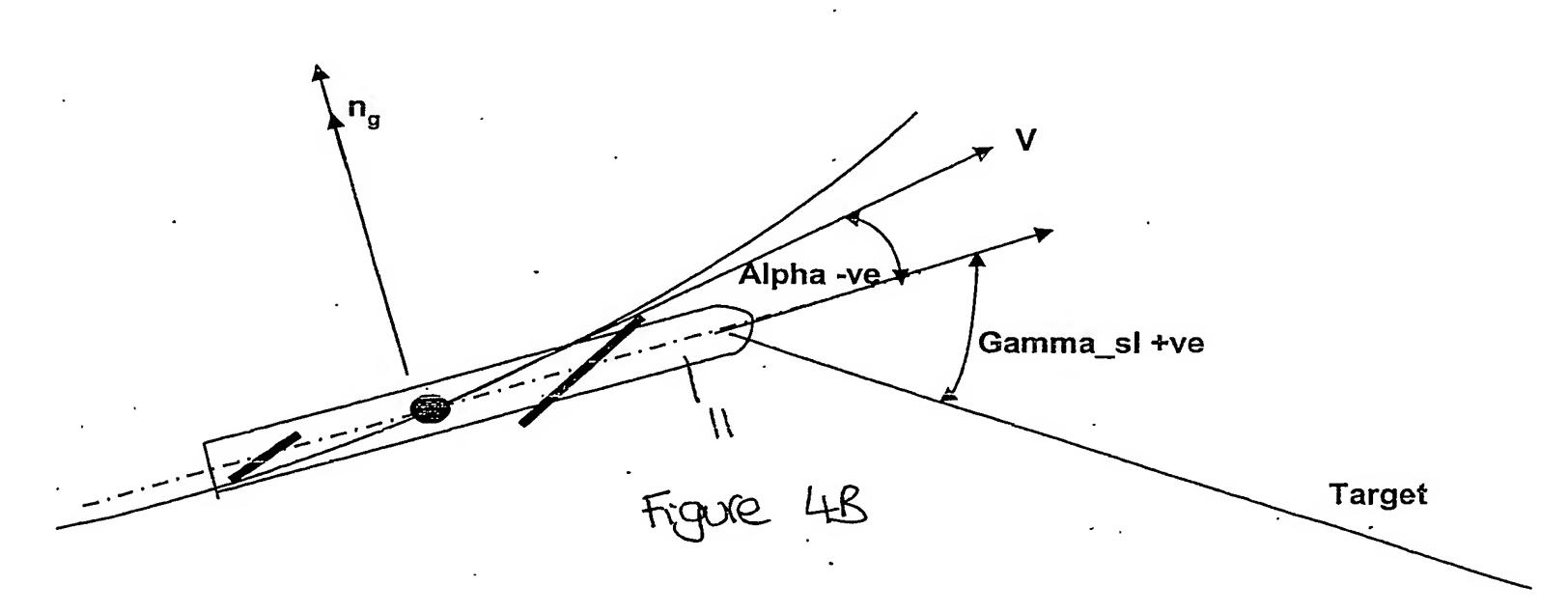
Figure 2B

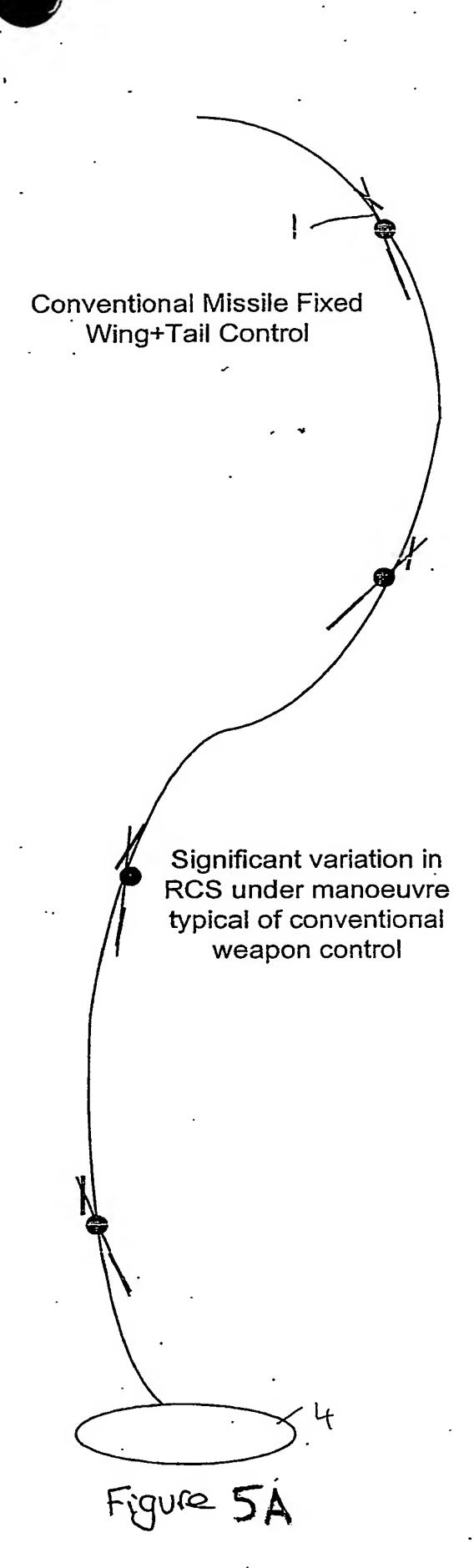
Figure 2B

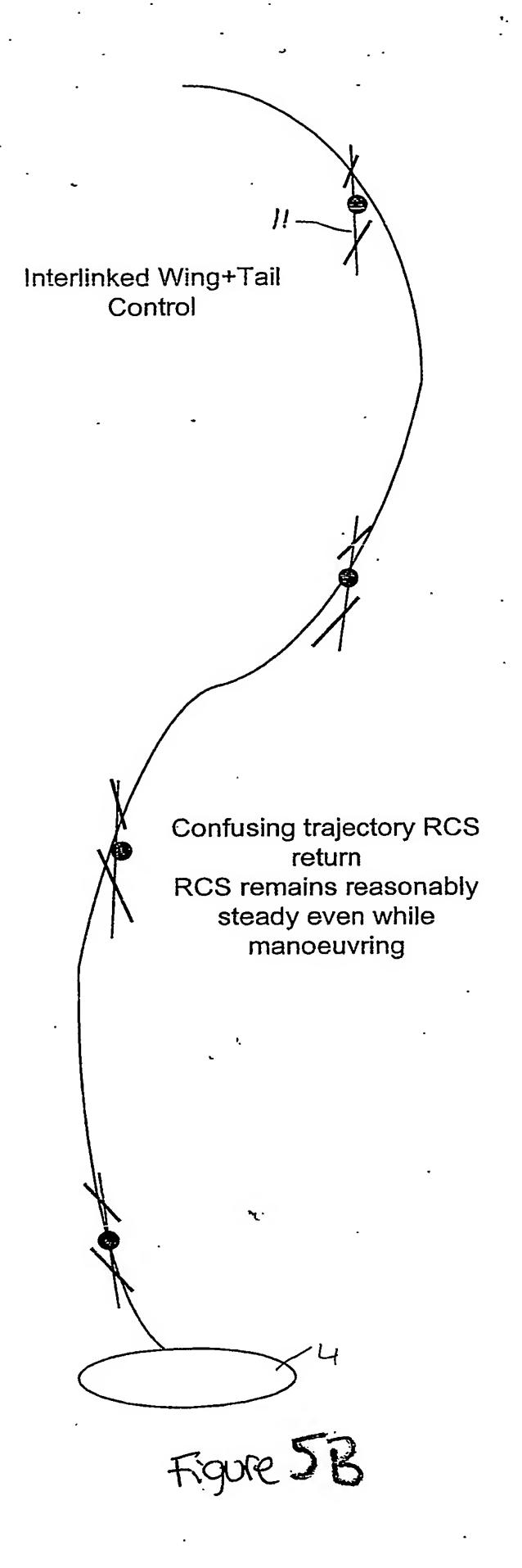
Missile re-aquires target Missile loses lock on pull-up look angle limit exceeded Acquisition

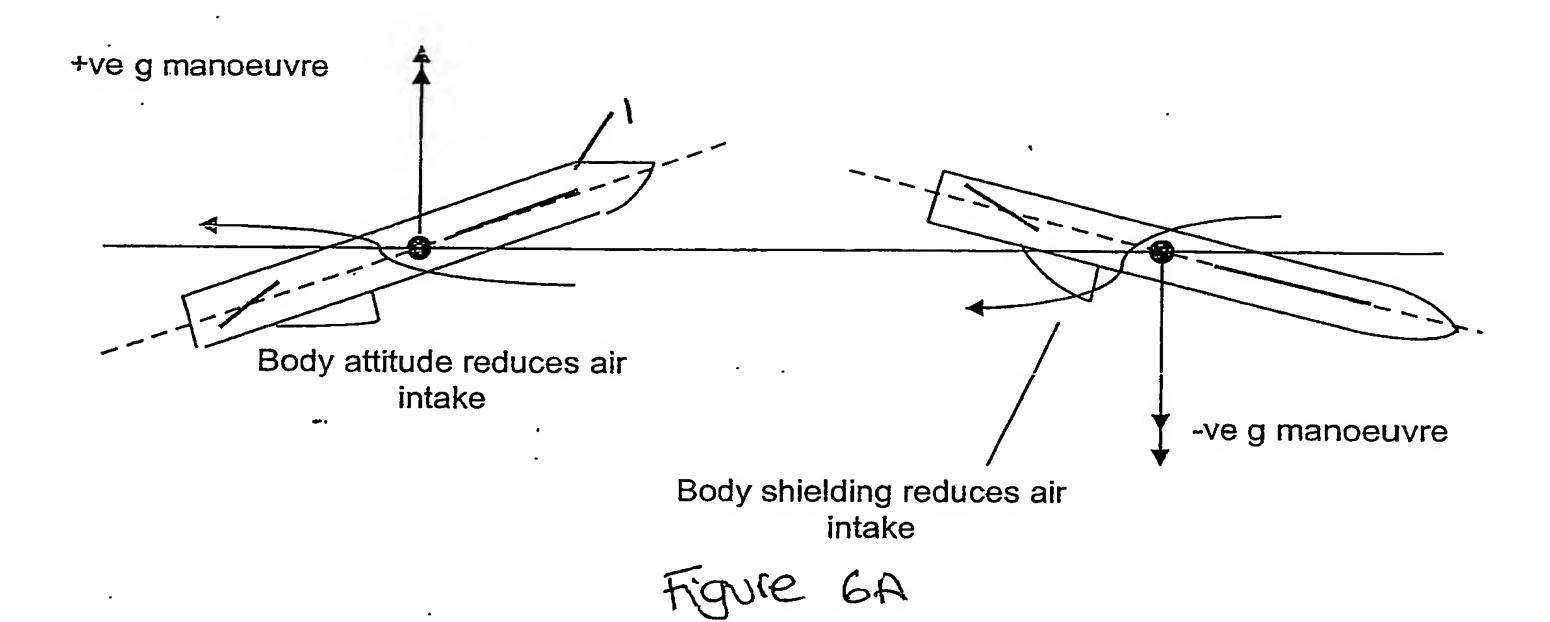












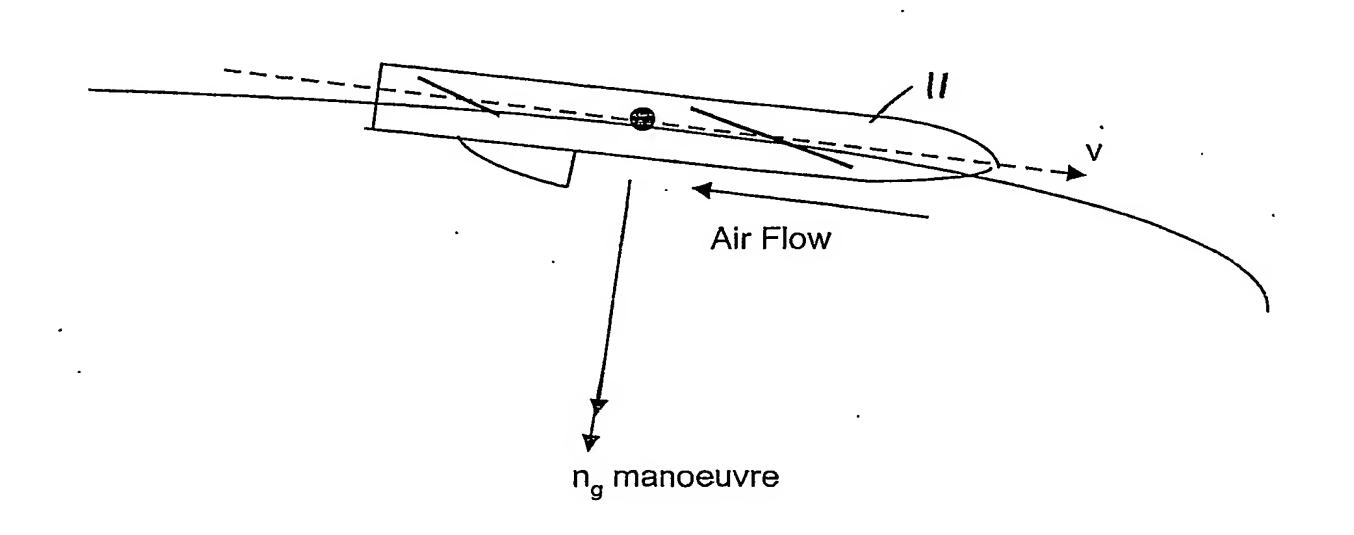


Figure GB

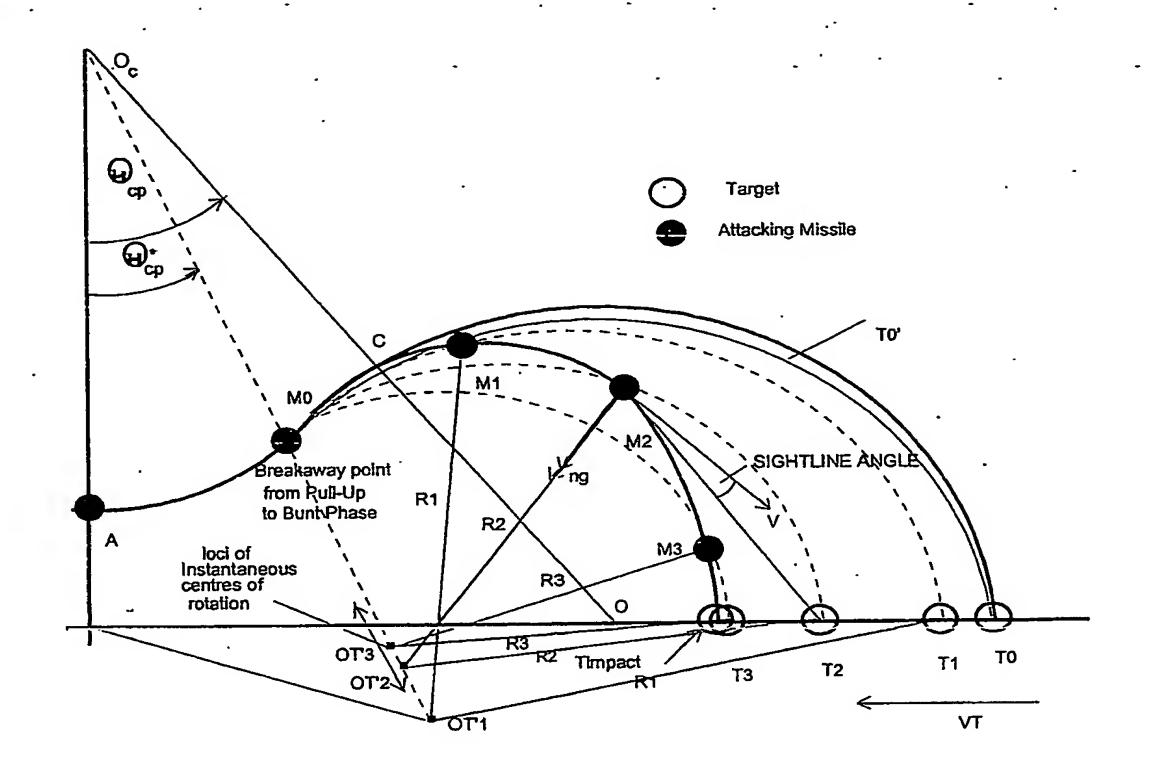
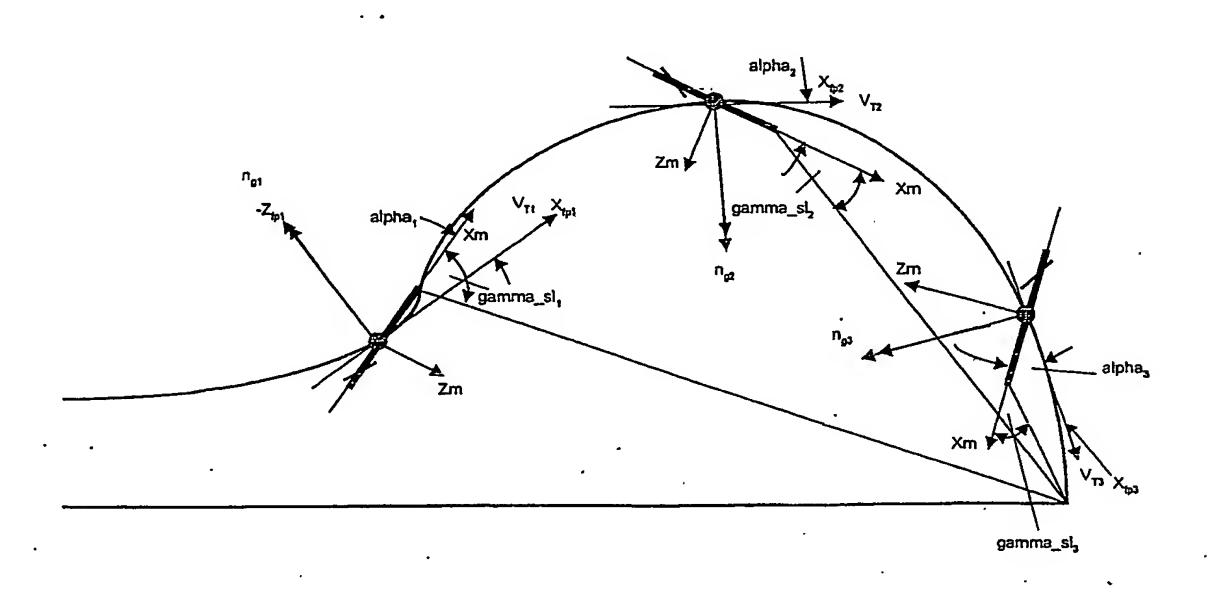


Figure 7



Figures

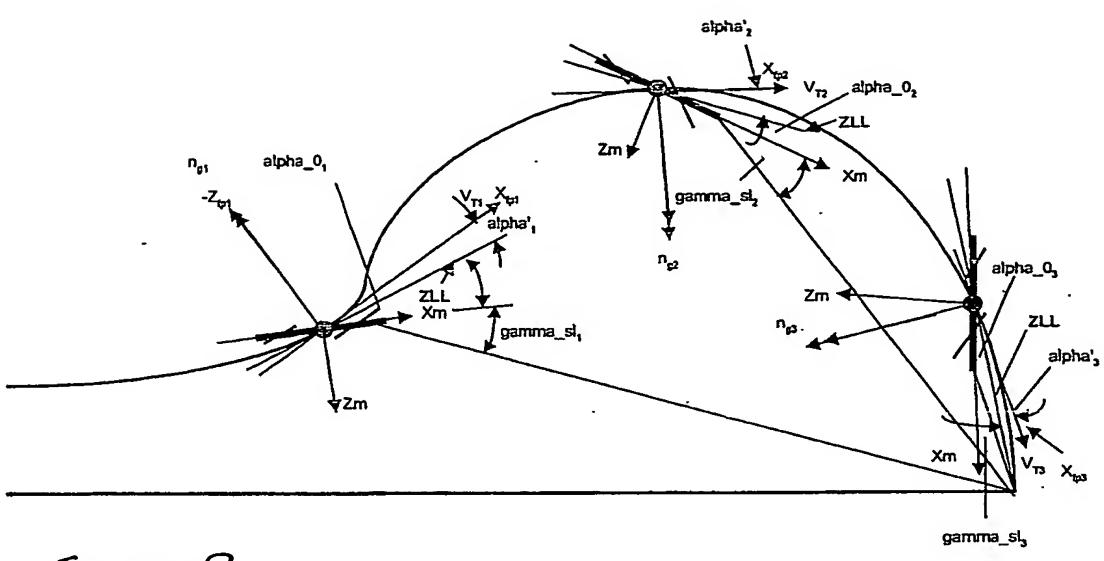


Figure 9

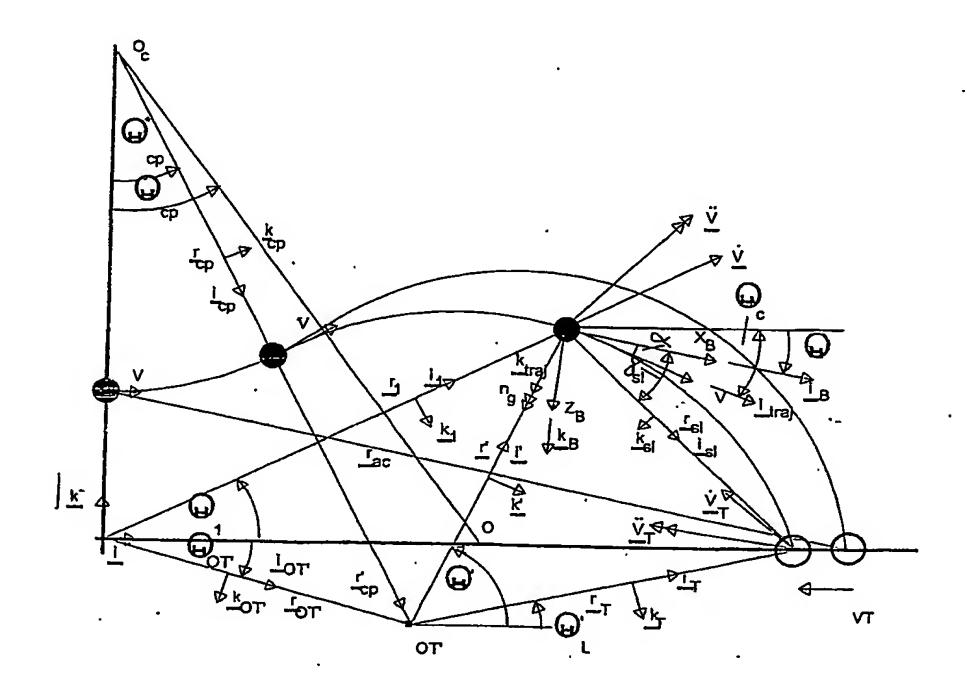
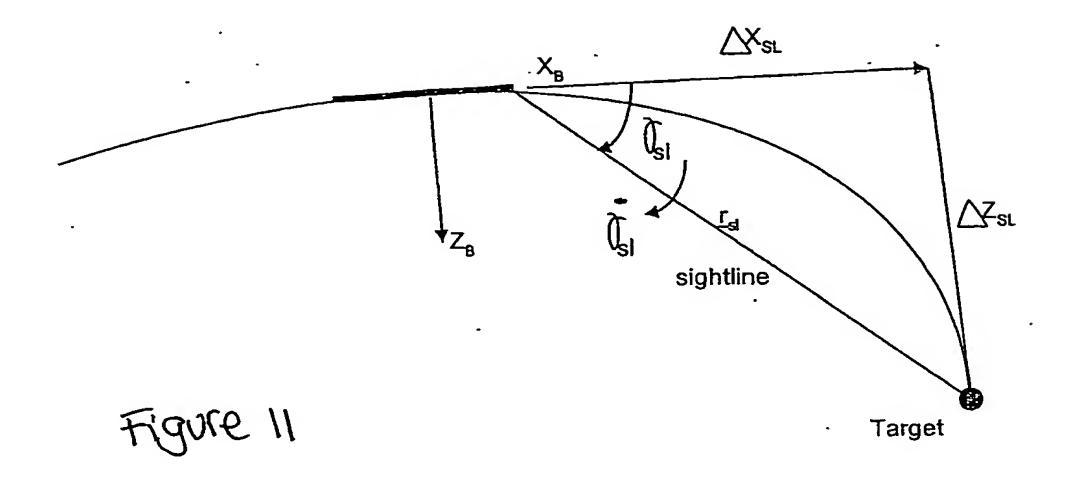


Figure 10



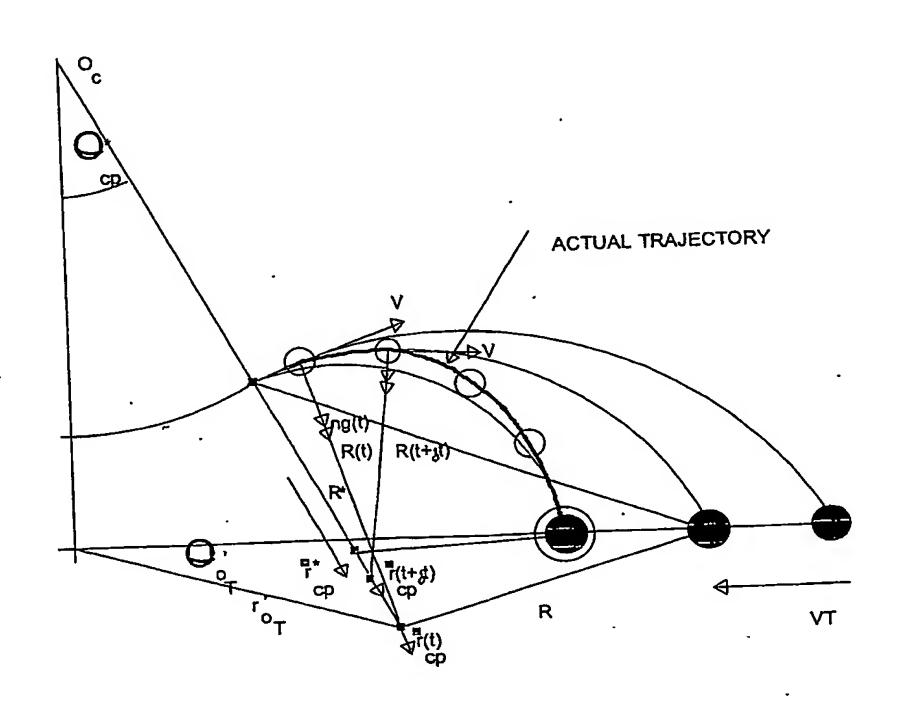


Figure 12

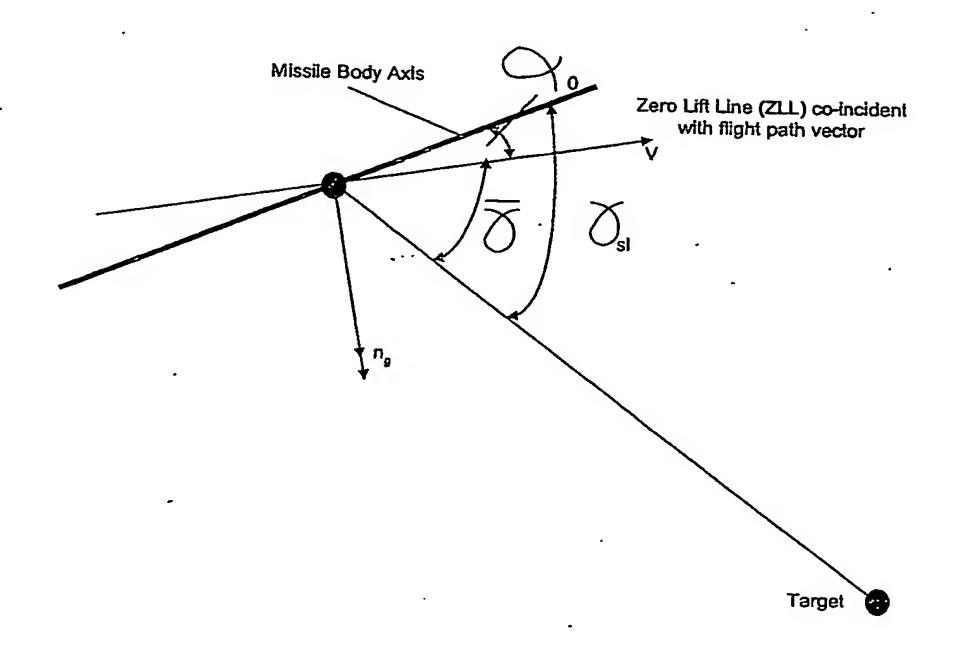
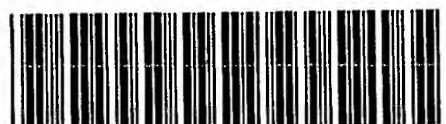


Figure 13

PCT/GB2004/001846



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